A photograph of a galaxy, likely the Milky Way, showing a bright star in the foreground. The galaxy's structure is visible, including the central bulge and the spiral arms. The star is bright and has a four-pointed diffraction pattern. The galaxy's color is a mix of blue and white, with some reddish-brown dust lanes. The background is dark with some faint stars.

From our Galaxy to
Distant DLAs: The
Condensation of
Gas-Phase
Elements onto
Interstellar Dust
Grains

Ed Jenkins

Princeton University Observatory

Logarithmic depletion of element X from the gas phase

$$[X/H] = \log\left(\frac{X}{H}\right)_{obs} - \log\left(\frac{X}{H}\right)_{stellar}$$

Reference
Abundance:
solar or B stars

Number density of
element X in dust relative
to hydrogen

$$(X_{dust}/H) = (X/H)_{\odot} \left(1 - 10^{[X_{gas}/H]}\right)$$

What has been Known for some Time

- Depletions vary from one location to the next
 - Sightlines with low average density $N(H)/d$ have less depletion
 - Gas at high velocity displacements have less depletion: grains have been disrupted
- Depletions vary from one element to the next
 - Depletion strengths are greatest for elements that can form refractory compounds and are small for those that can only form volatile compounds

An Interpretation of Milky Way ISM Gas-Phase Abundances Reported in the Literature

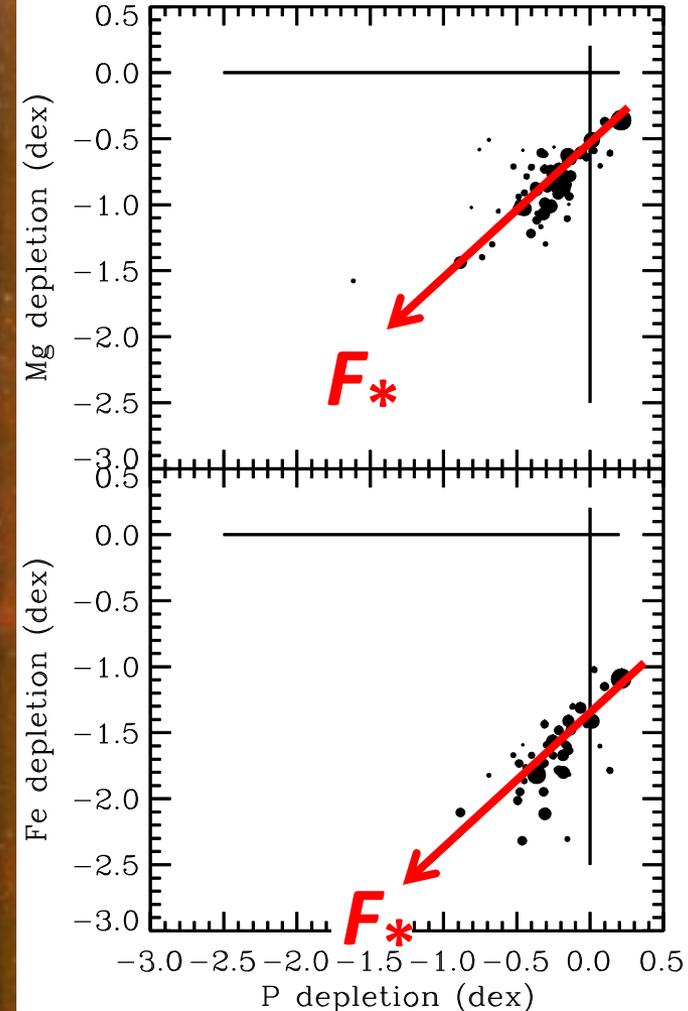
- **Basic Tactic:**
 - Adopt protosolar abundances as a reference standard
 - Ignore the sightline properties and characterize depletions of elements with respect to each other, recognizing that the severity of depletions differ from one element to the next and from one region of space to the next.

Published by Jenkins (2009: ApJ, 700, 1299)

Underlying Strategy

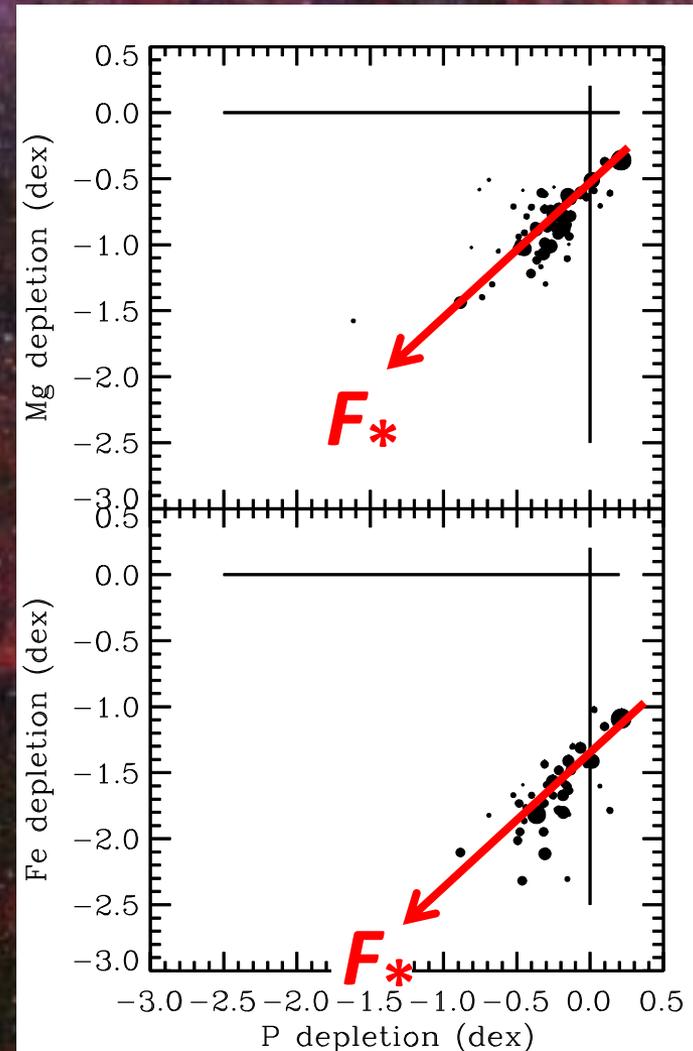
- Basic premise:
 - All elements deplete together in some systematic fashion, but by differing degrees that change from one region to another and from one element to the next.
 - Propose a single parameter, F_* , that expresses a general level of depletion along a sight line.

(F_* is much like $\langle n(\text{H}) \rangle$ that has been used in the past.)



Underlying Strategy

- Another basic premise:
 - Differences in how the elements respond to changes in F_* are represented by other parameters specific to each element.

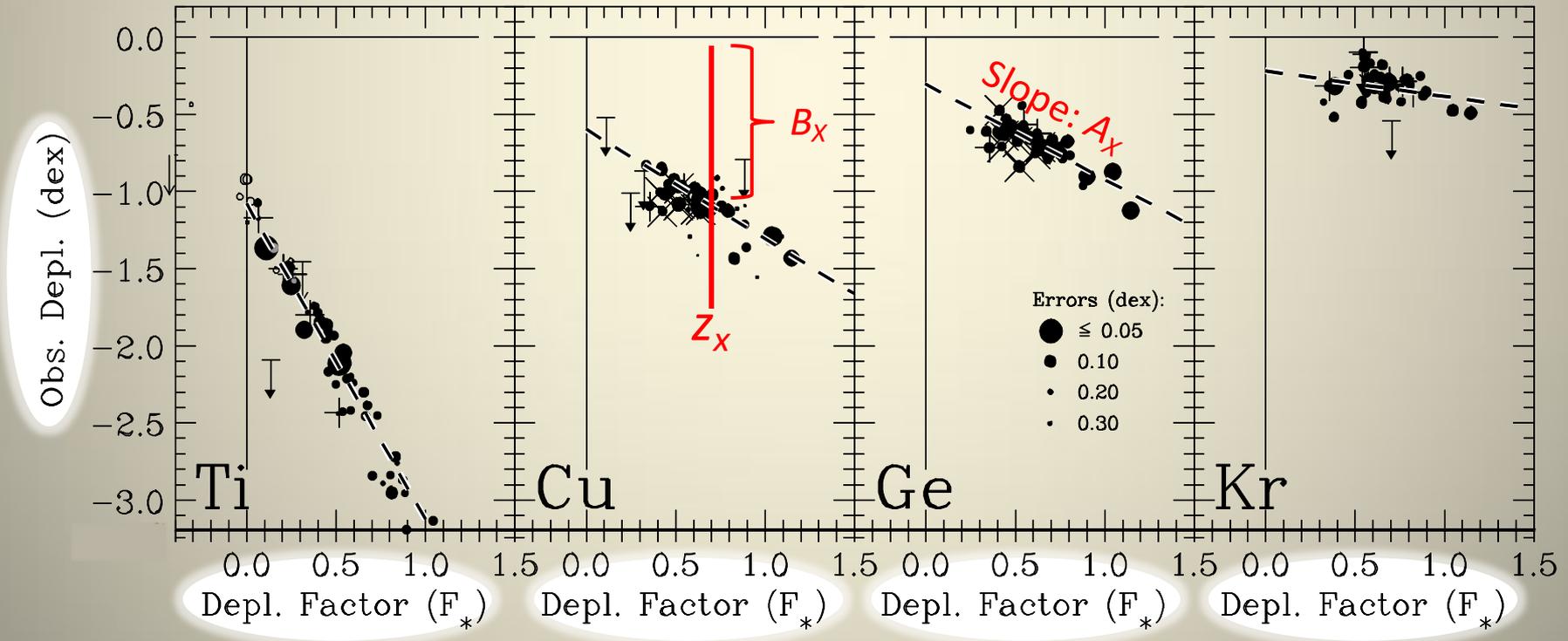


Basic Equation

For element X:

Logarithmic Depletion factor

$$[X_{gas} / H] = B_X + A_X (F_* - z_X)$$

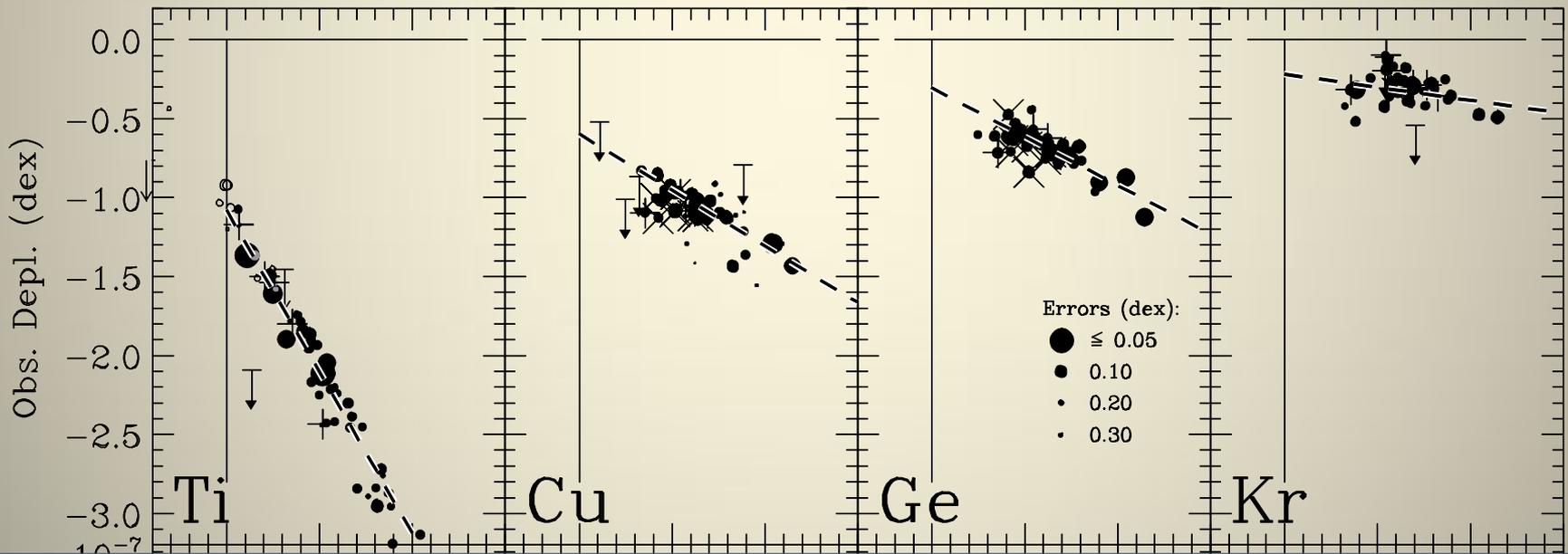


The Buildup of Dust Grains

Conventional Formula:

$$(X_{dust} / H) = (X/H) (1 - 10^{-|A_x| [X_{gas} / H]})$$

$|A_x|$ is a rate constant for element condensation



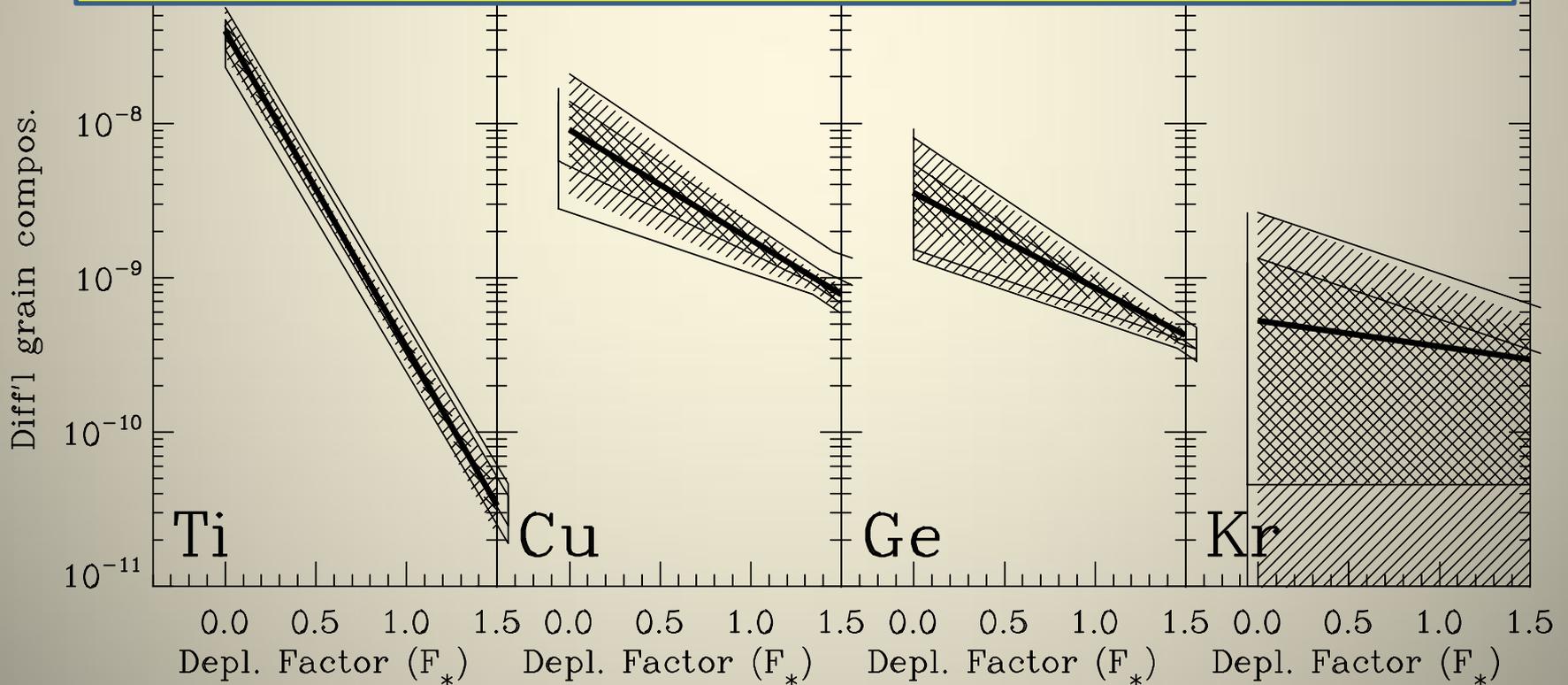
The Buildup of Dust Grains

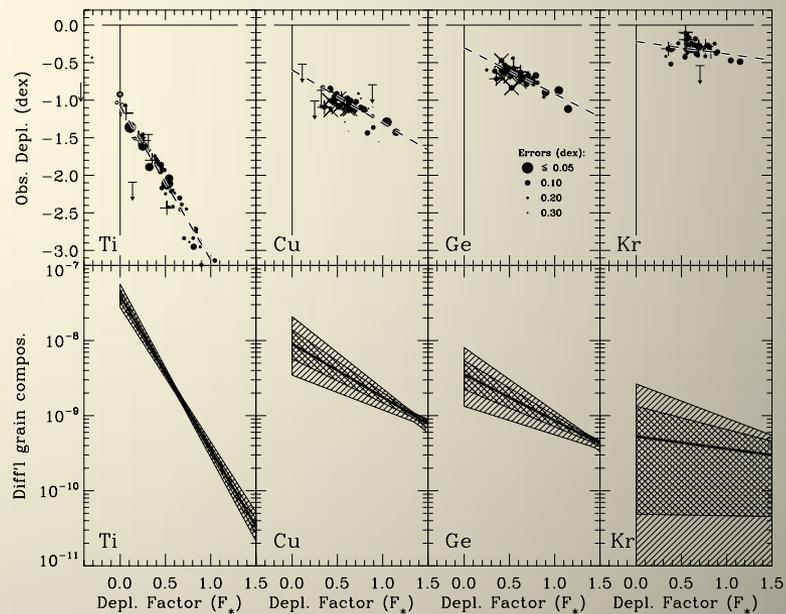
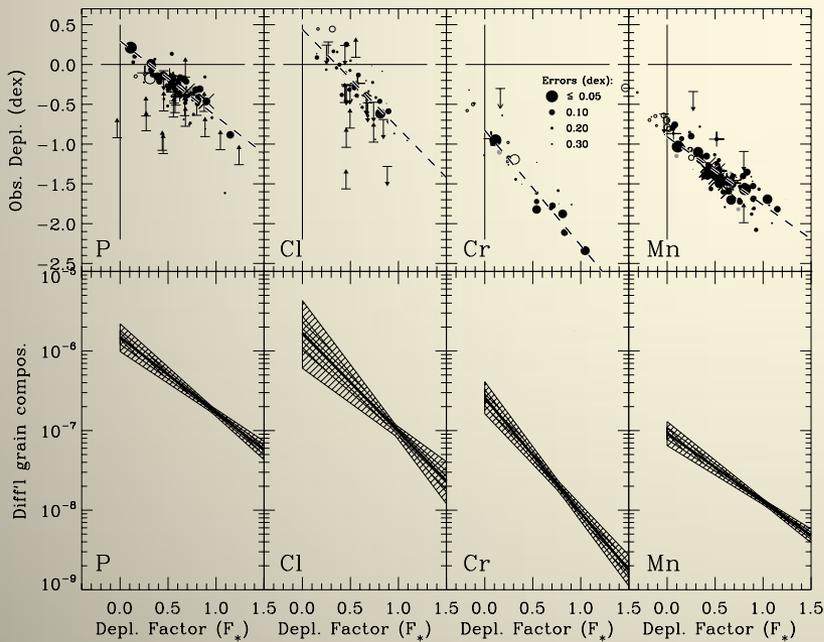
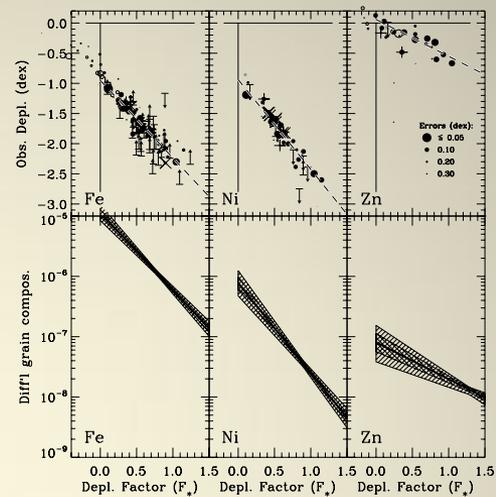
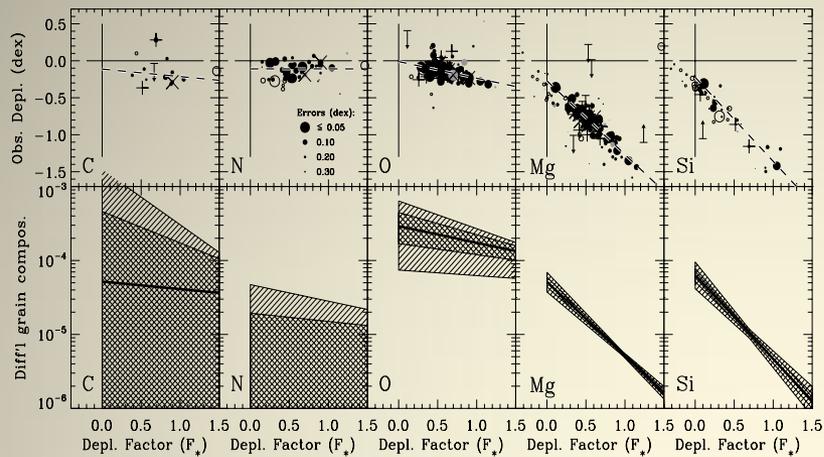
Differential Element Contributions:

$$\frac{d(X_{dust} / H)}{dF_*} = -(\ln 10) A_X (X_{gas} / H) F_*$$

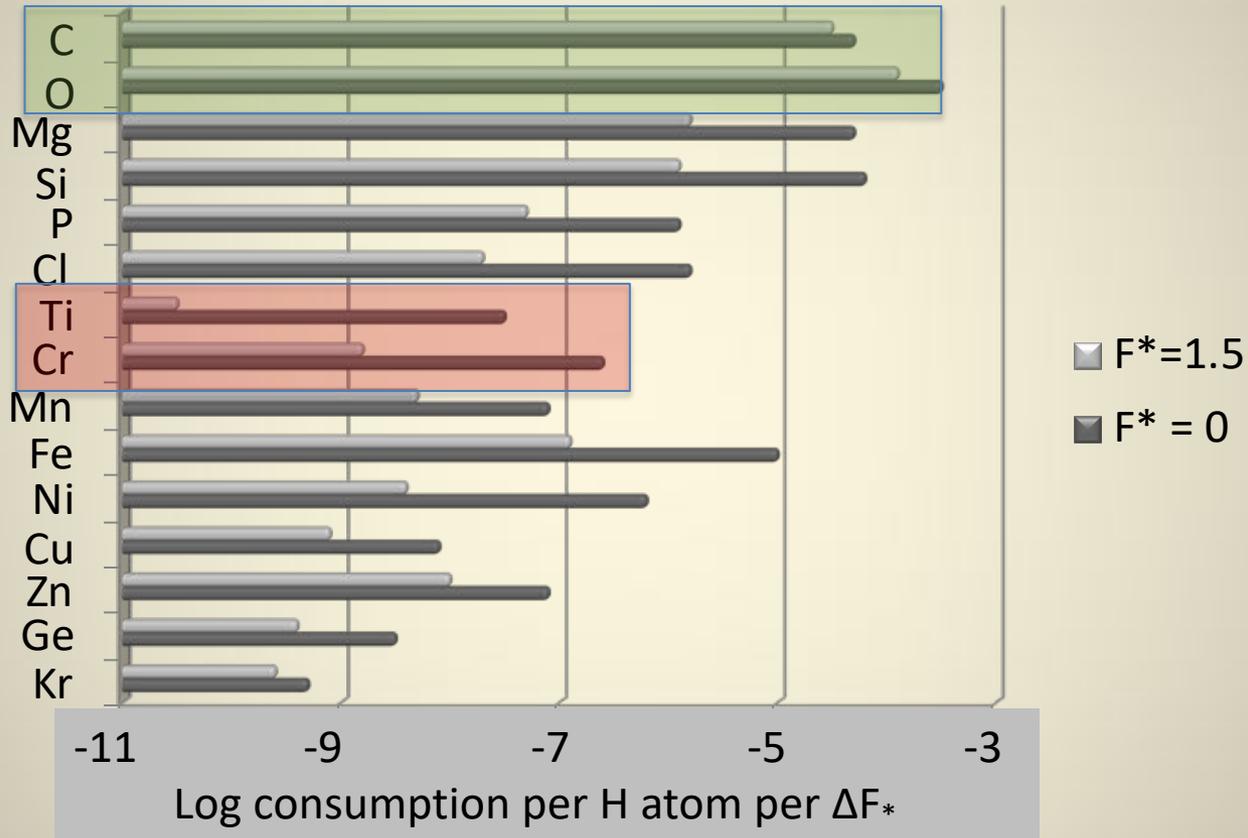


$|A_X|$ is a rate constant for element condensation





Summary of Element Consumption Rates



**(Mass of elements in dust)/(total element mass) = 0.20 ($F_* = 0$)
0.54 ($F_* = 1$)**

Average Density of Dispersed Solids

Refractive index at low freq.

Number of grains per unit area
in a column of length d

Radius of each grain

Optical
depth over
a distance d

Grain volume
Internal
density

Extinction
efficiency factor

$$\int_0^{\infty} Q_e d\lambda = 4\pi^2 a \left(\frac{m^2 - 1}{m^2 + 2} \right)$$

$$\langle \rho_g \rangle = \frac{N_g}{d} \times \frac{4\pi a^3}{3} \times \rho_s$$

$$N_g = \left(\frac{\int_0^{\infty} \tau d\lambda}{4\pi^3 a^3} \right) \left(\frac{m^2 + 2}{m^2 - 1} \right)$$

$$\langle \rho_g \rangle = \frac{1}{3\pi^2} \times \frac{\int_0^{\infty} \tau d\lambda}{d} \times \left(\frac{m^2 + 2}{m^2 - 1} \right) \times \rho_s$$

An application of
the Kramers-
Kronig
dispersion
relation by
Purcell (1969,
ApJ, 158, 433)

Average Density of Dispersed Solids

Combine $A_V = 1.8 \text{ mag kpc}^{-1}$
with relative extinctions from
1000 Å to 20 μm

Compare
with Z/X in
the Sun

≈ 3

≈ 2 for most
substances

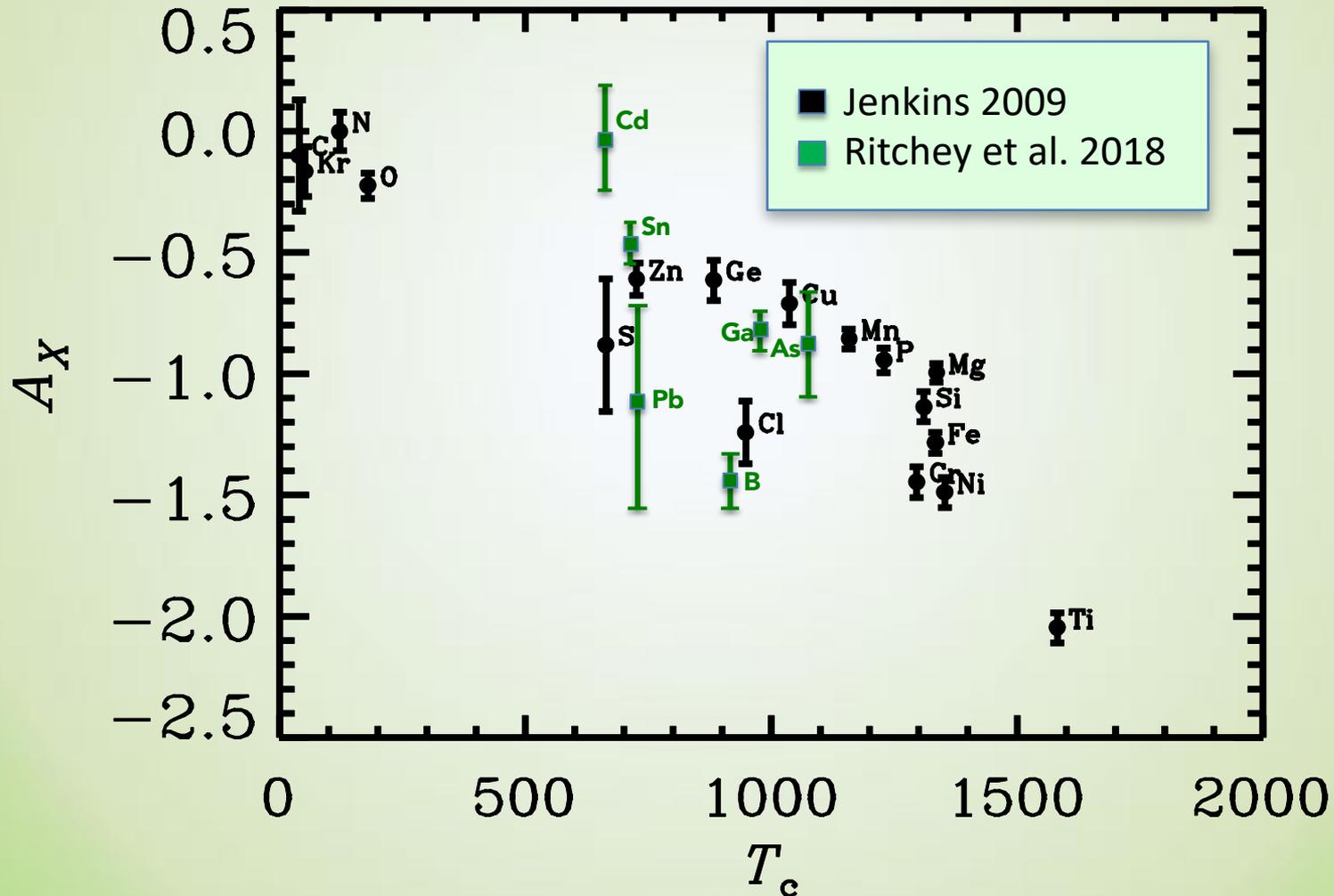
0.018

$$\langle \rho_g \rangle = 1.8 \times 10^{-26} \text{ g cm}^{-3} = 0.006 \langle \rho_H \rangle$$

$$\langle \rho_g \rangle = \frac{1}{3\pi^2} \times \left(\frac{\int_0^\infty \tau d\lambda}{d} \right) \times \left(\frac{m^2 + 2}{m^2 - 1} \right) \times \rho_s$$

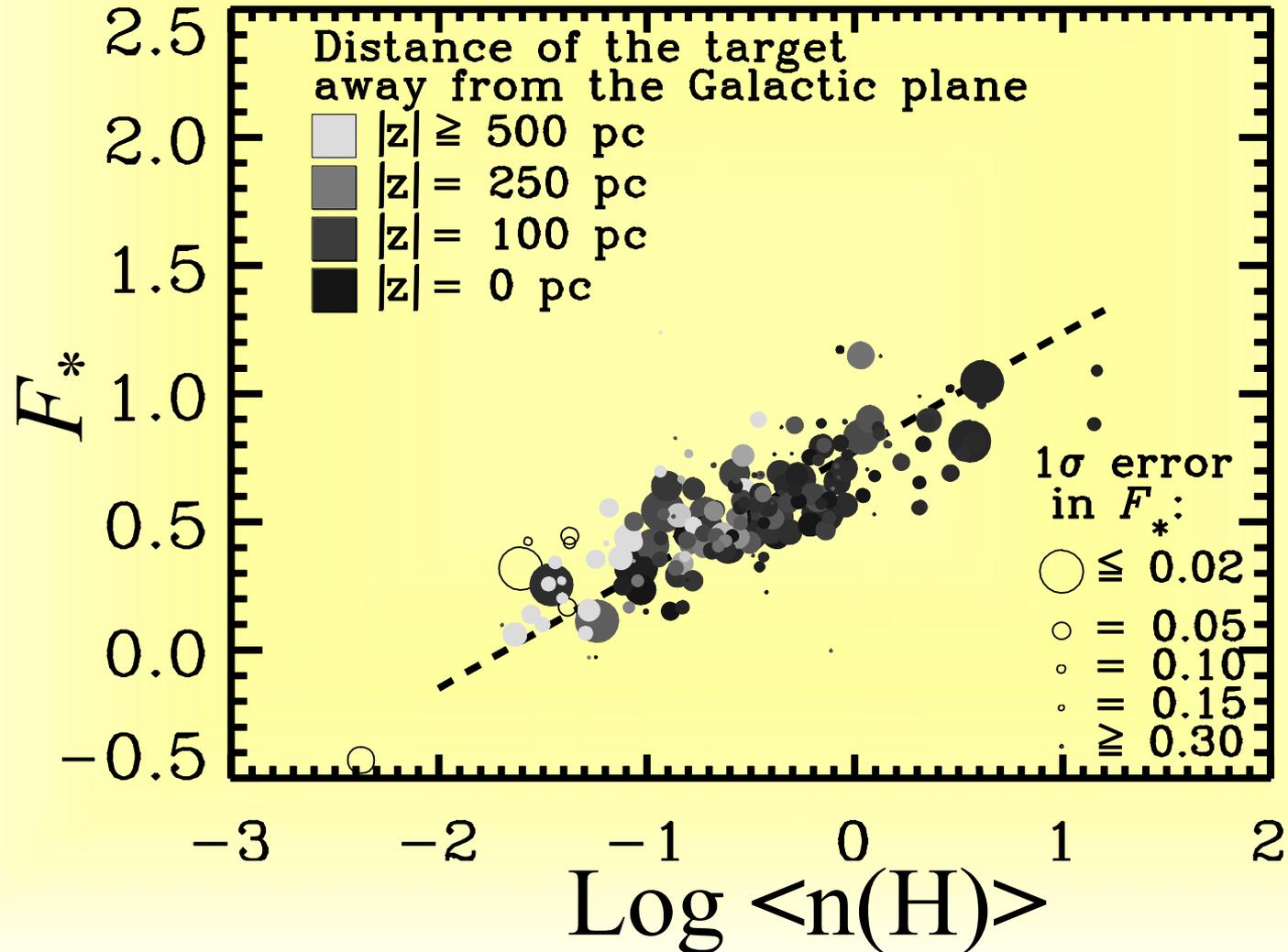
(Mass of elements in dust)/(total element mass) = 0.20 ($F_* = 0$)
0.54 ($F_* = 1$)

Depletion Trends against Condensation Temperatures

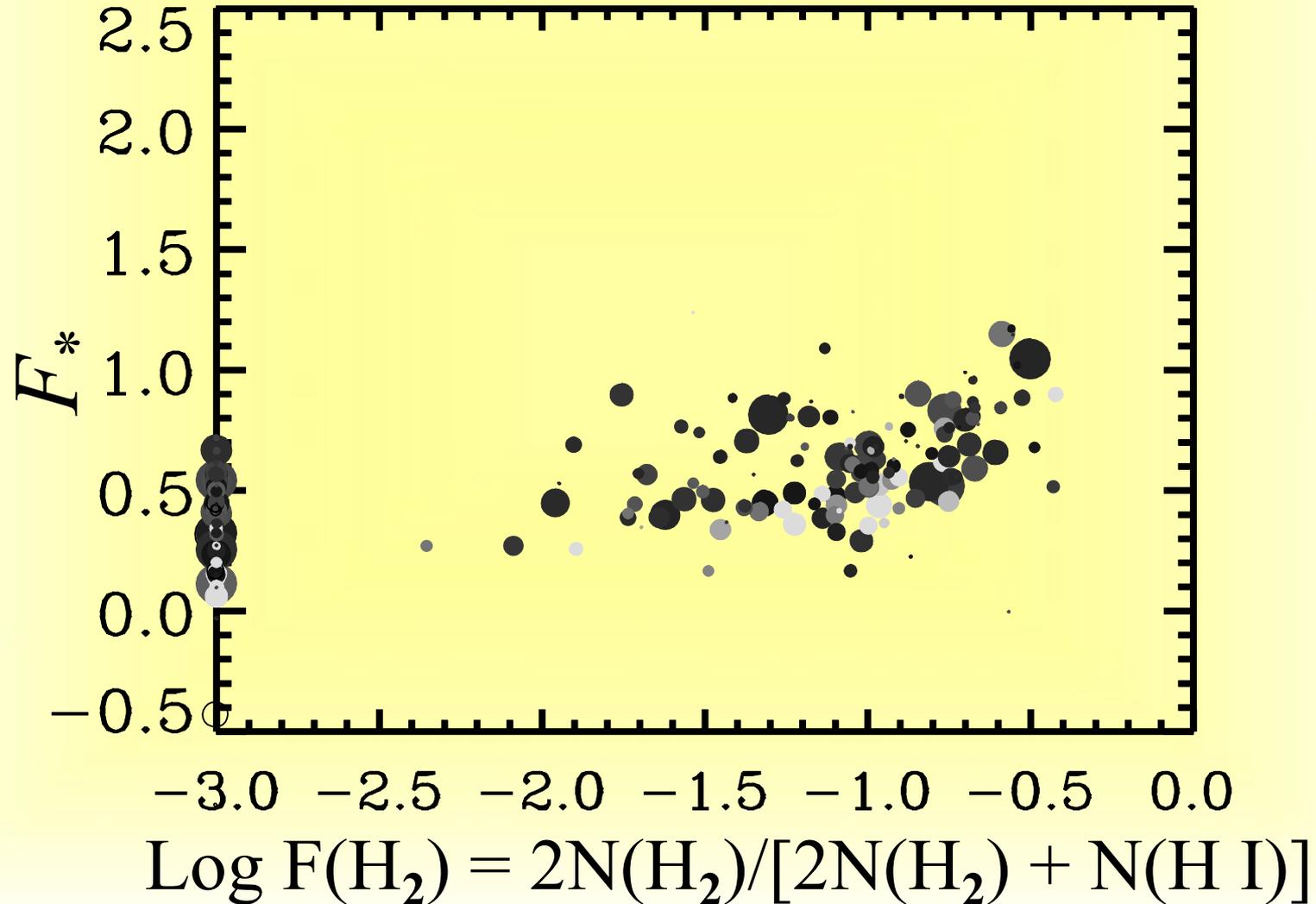


Sightlines

Trends of Overall Depletion Strengths



Trends of Overall Depletion Strengths



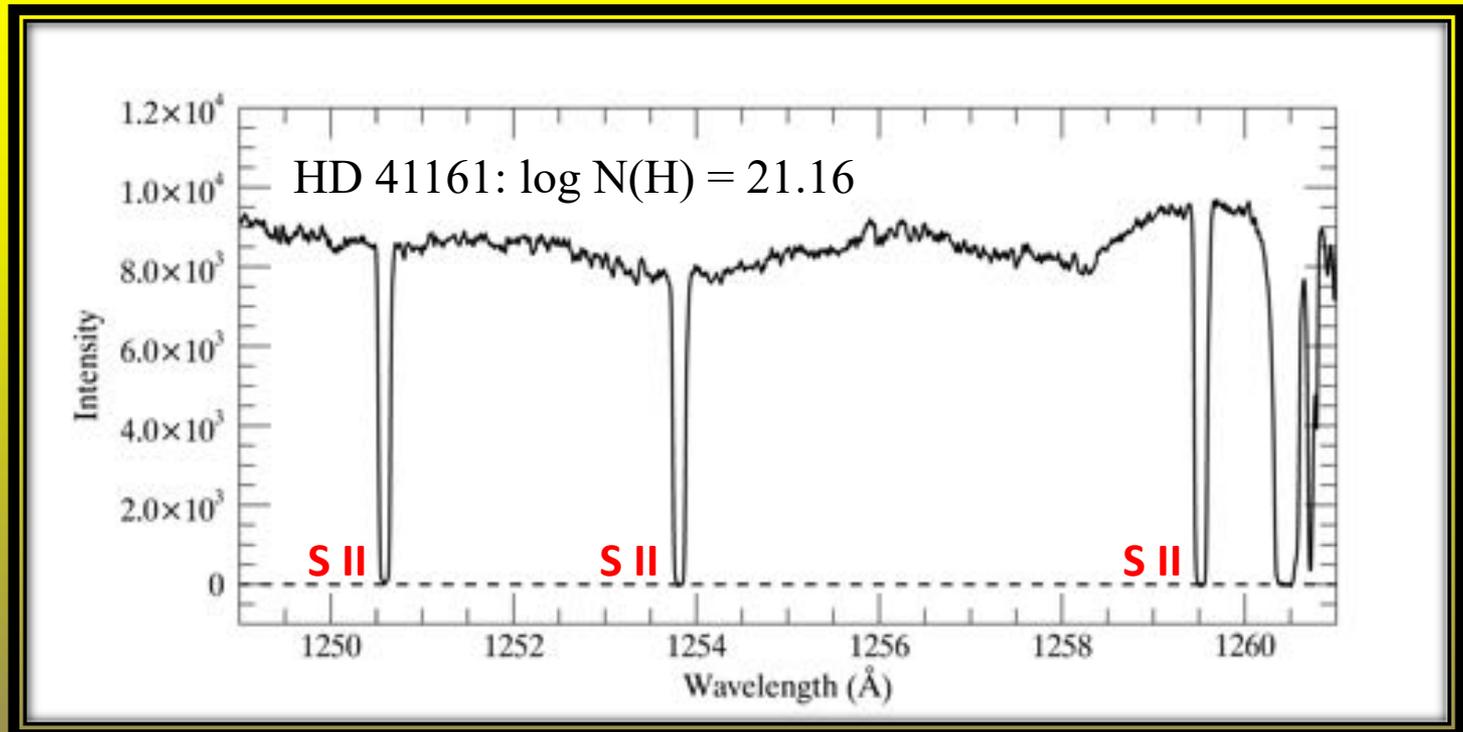
Some Notes about Specific Elements

Three noteworthy cases:

S, O, and Kr

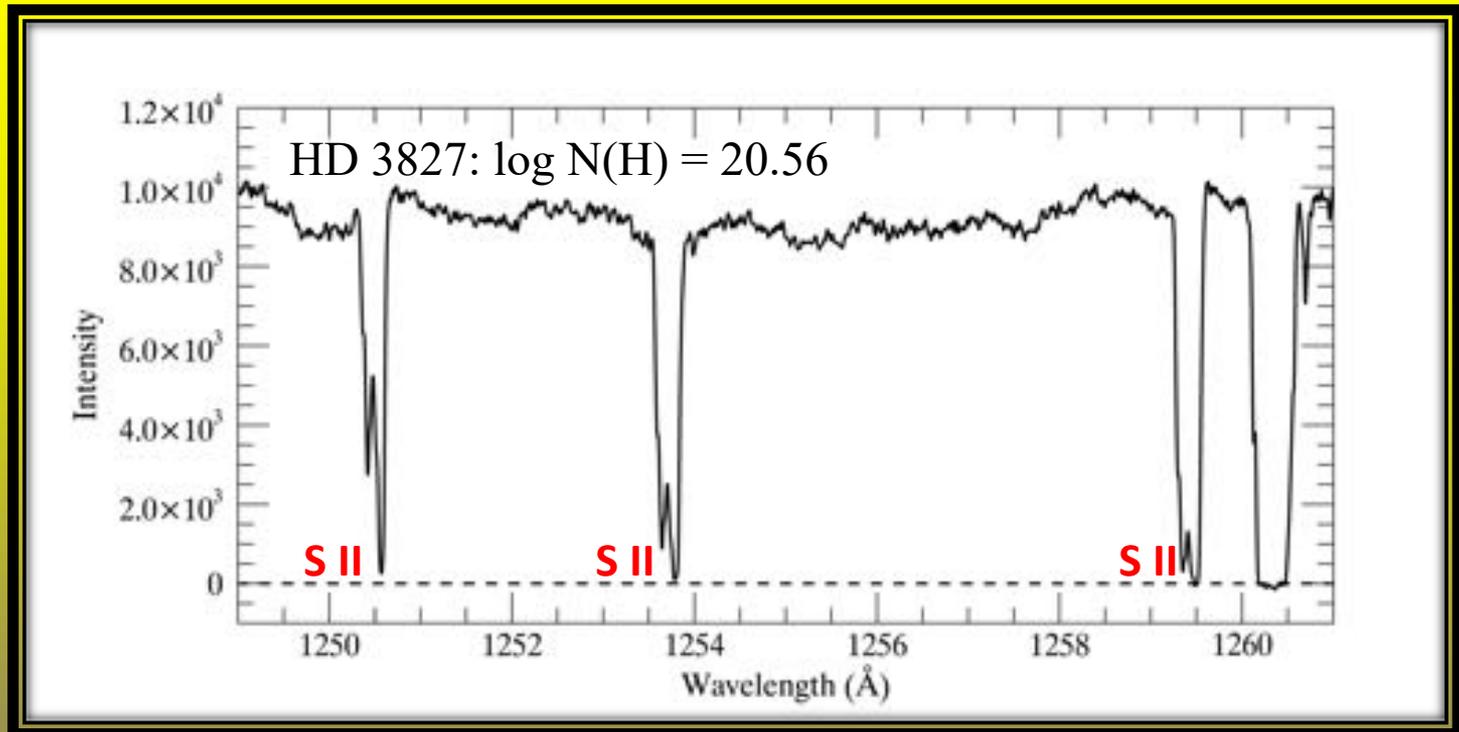
Sulfur

- A problem element: many investigators have proposed that S is undepleted.
- Results may be misleading ...



Sulfur

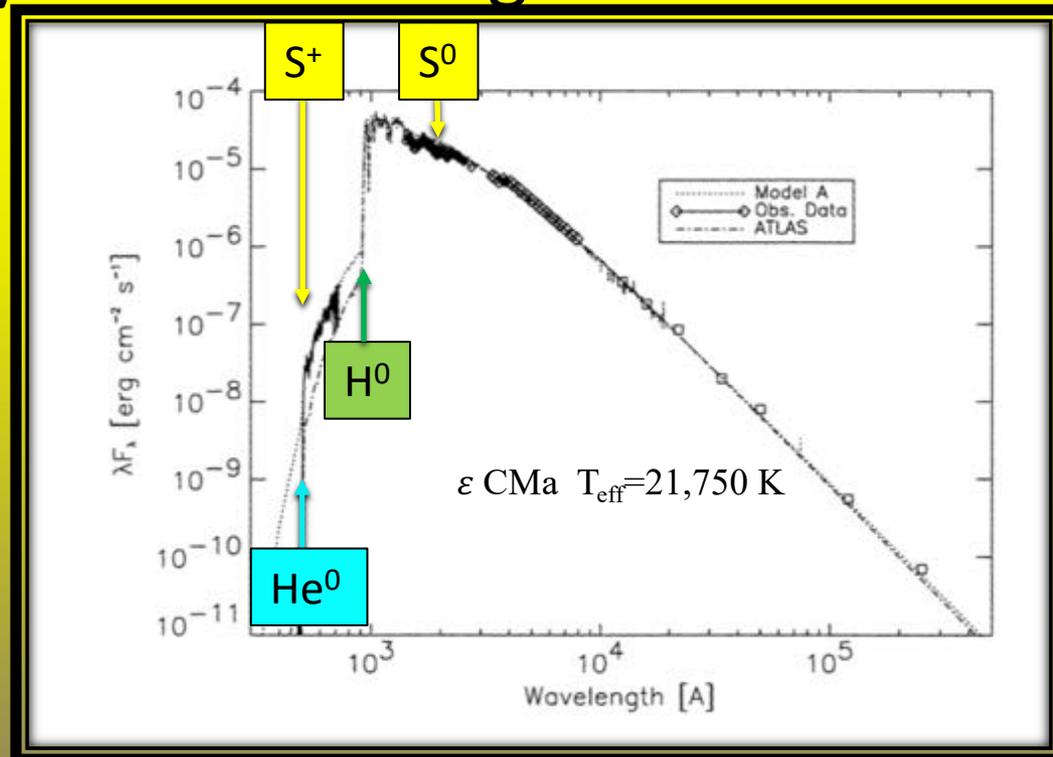
- A problem element: many investigators have proposed that S is undepleted.
- Results may be misleading ...



Sulfur

- A problem element: many investigators have proposed that S is undepleted.
- Results may be misleading ...

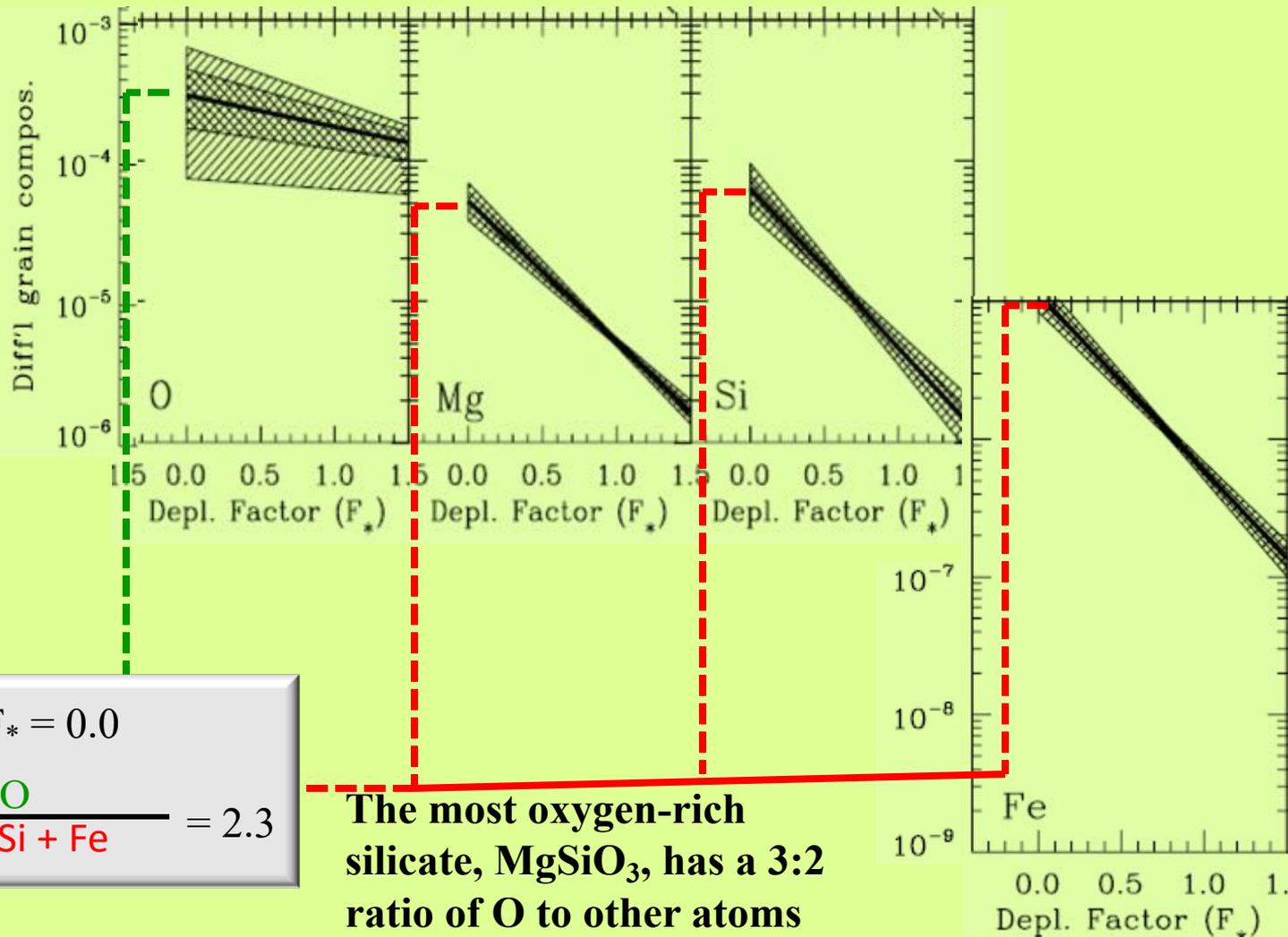
Inside the star's H II region, H is fully ionized, but S is only singly ionized. This can raise the amount of S II without increasing H I.



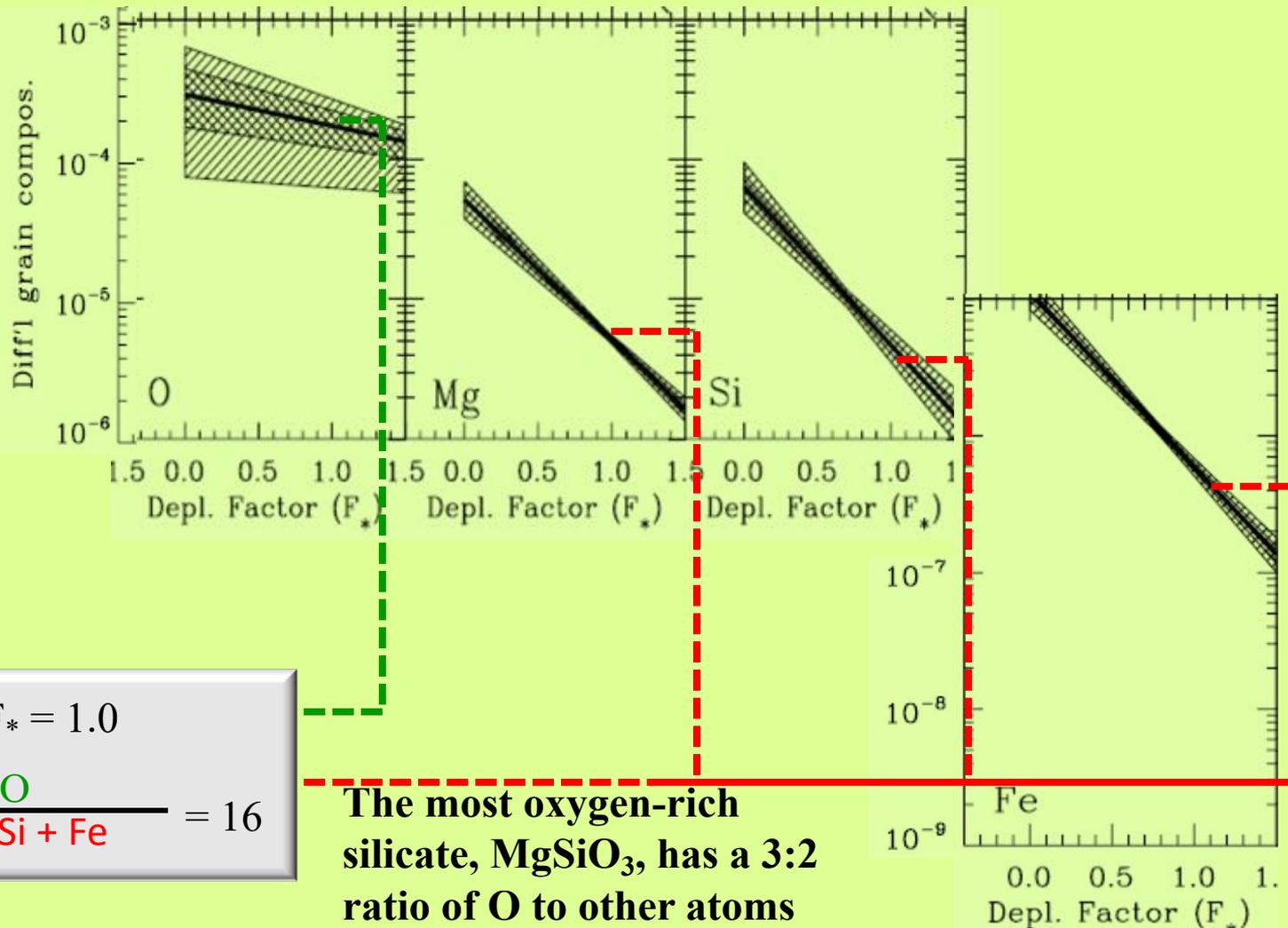
The Consumption of Oxygen Compared to other Elements

- Conventional view: oxygen is mostly incorporated into refractory compounds such as silicates and oxides.
- Let's examine whether or not this is consistent with our determinations of $d(X_{\text{dust}}/H)/dF_*$

The Consumption of Oxygen Compared to other Elements

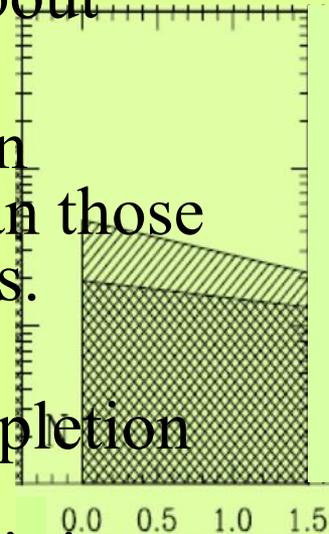


The Consumption of Oxygen Compared to other Elements

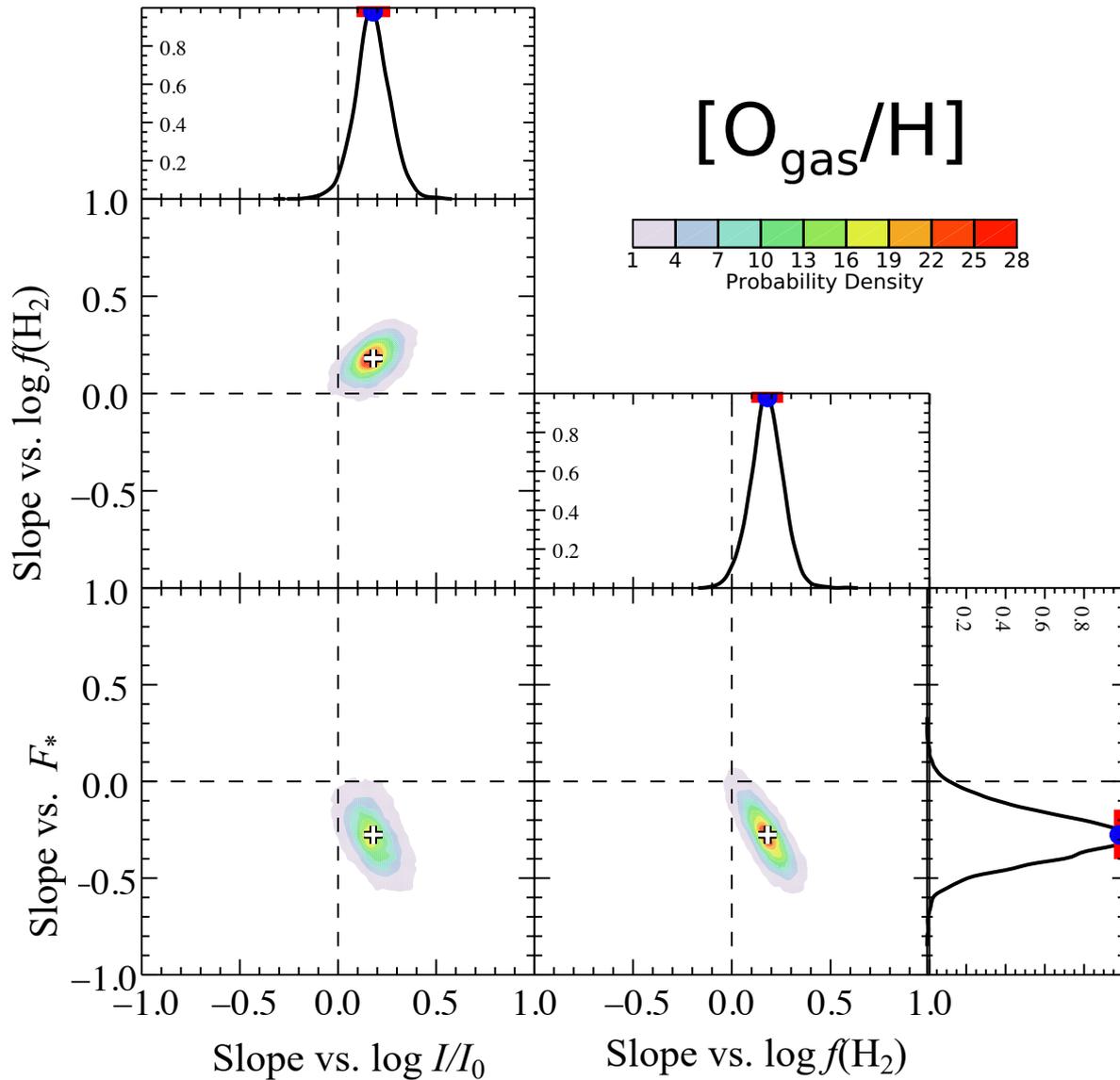


The Consumption of Oxygen Compared to other Elements

- Conclusion: In addition to forming silicates, O must deplete by forming some other compound using another abundant element.
 - Various oxides of N? Unlikely, since N does not seem to deplete (at least not appreciably more than about 10^{-5} per H atom per unit change in F_*).
 - H₂O? Perhaps, but 3.05 μm ice feature only seen toward regions with extinctions much larger than those of the lines of sight in the UV absorption studies.
 - CO, CO₂ and O₂ are present in the ISM, but in amounts that are not sufficient to explain the depletion of O.



Perhaps very large grains (diam. $\gg 1\mu\text{m}$) containing appreciable amounts of H₂O are present but not visible?



Interpretation:

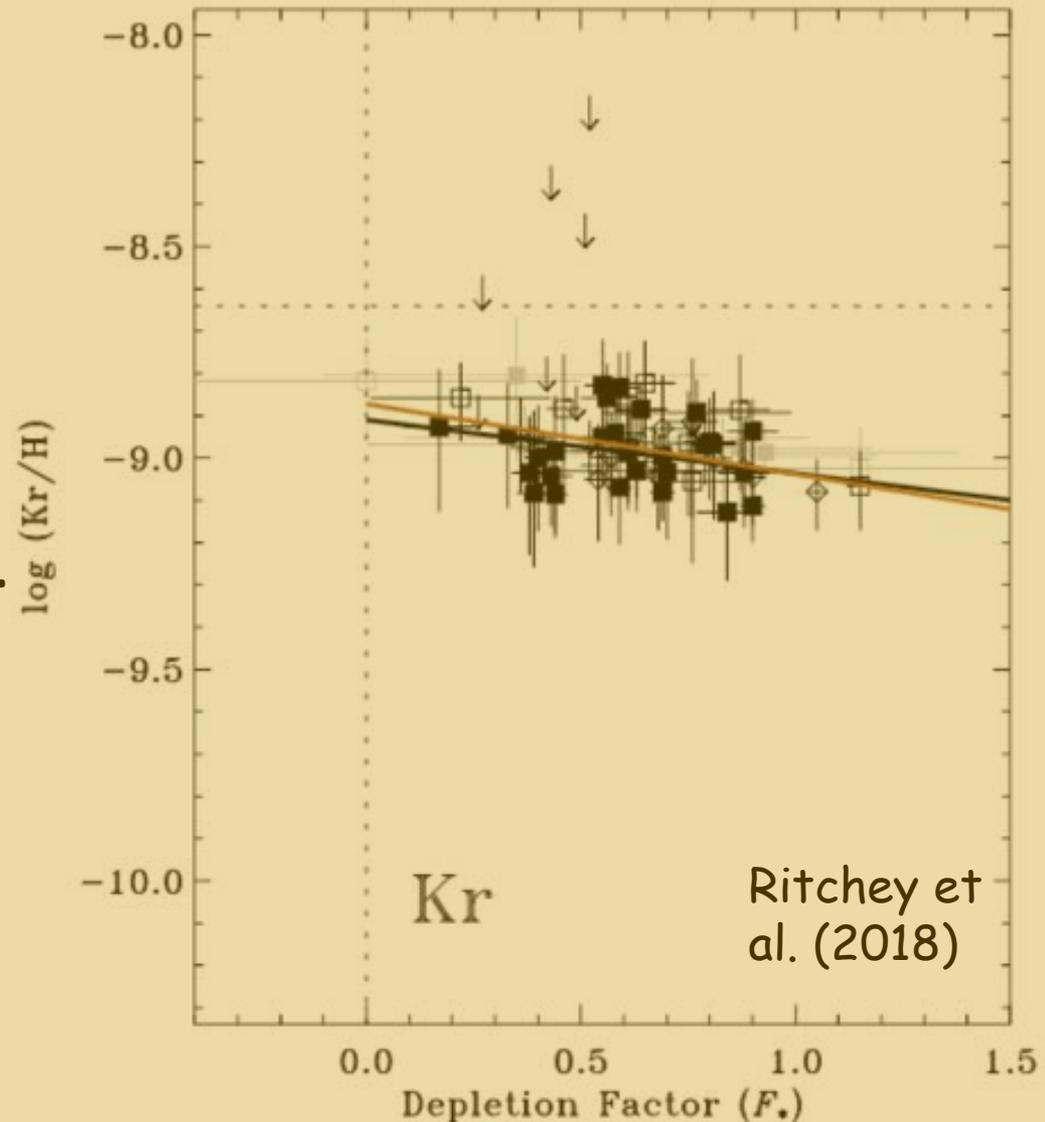
- Negative correlation with F_* no surprise, O follows other elements.
- Positive correlation with $f(H_2)$ seems counterintuitive: stronger molecular environment might favor reactions that create O-bearing molecules

A conjecture:

- $f(H_2) \propto n_H n_g / I = \text{func}(F_*) / I$
- If we could hold F_* and I constant, we'd expect $f(H_2)$ to also remain constant.
- A variation in $[O_{\text{gas}}/H]$ with $f(H_2)$ indicates some factor(s) other than just F_* and I may influence $f(H_2)$ – perhaps grain size distribution, where surface to volume ratios could influence production efficiency.

Krypton

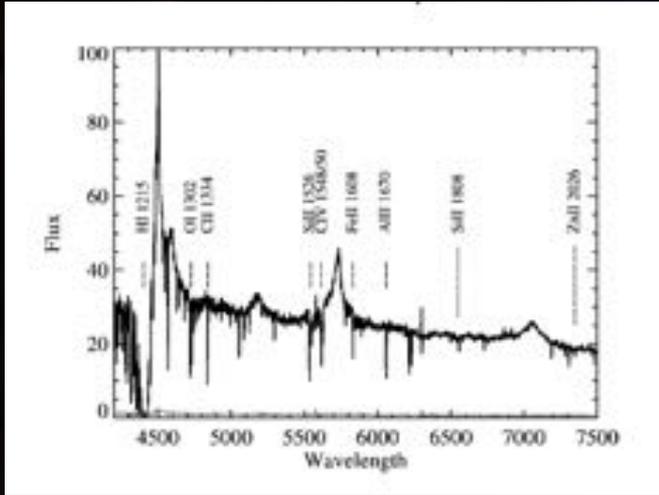
- Chemically inert
- However, meteoritic studies and laboratory experiments indicate that heavy noble gases can bind to solids via enhanced physisorption.
- A negative correlation with I/I_0 may arise from the creation of active binding sites by UV radiation.



Distant Absorption Line Systems

Basic Issues:

1. Absorption features in the spectrum of the quasar reveal column densities of the gas phases of various heavy elements and hydrogen.
2. Using the relationships of depletions seen in our Galaxy, can we interpret these outcomes in terms of a division between gas-phase and solid-phase abundances?



Background
Quasar

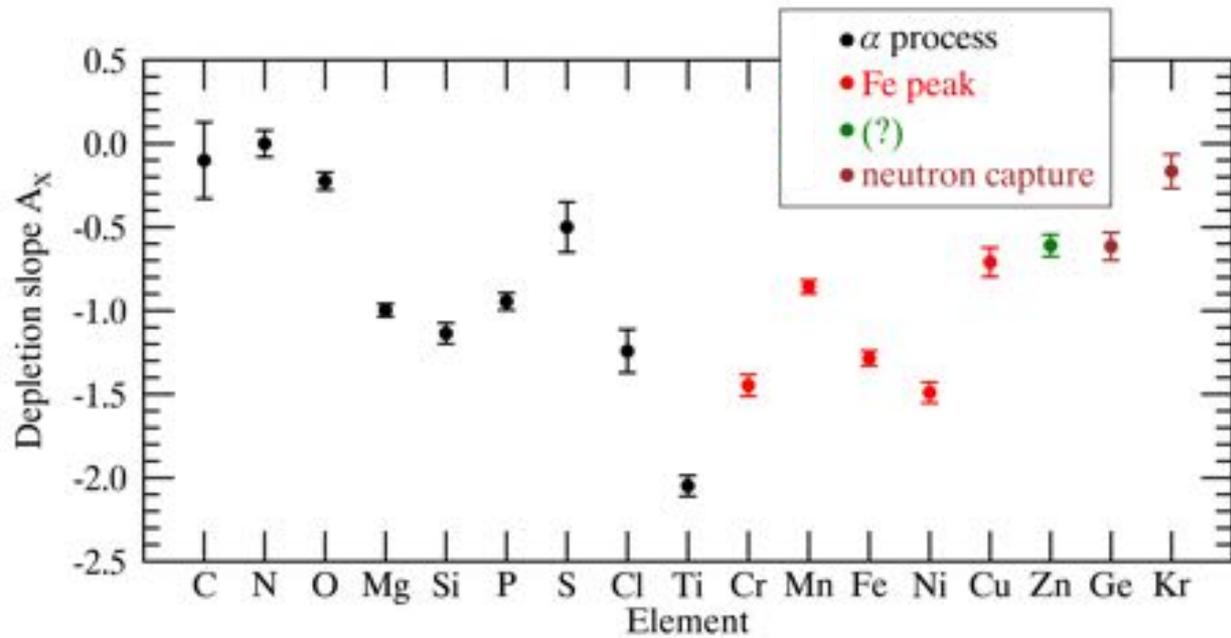
Galaxy that produces
a Damped Lyman- α
(DLA) absorption
system in the quasar
spectrum

Our Objectives

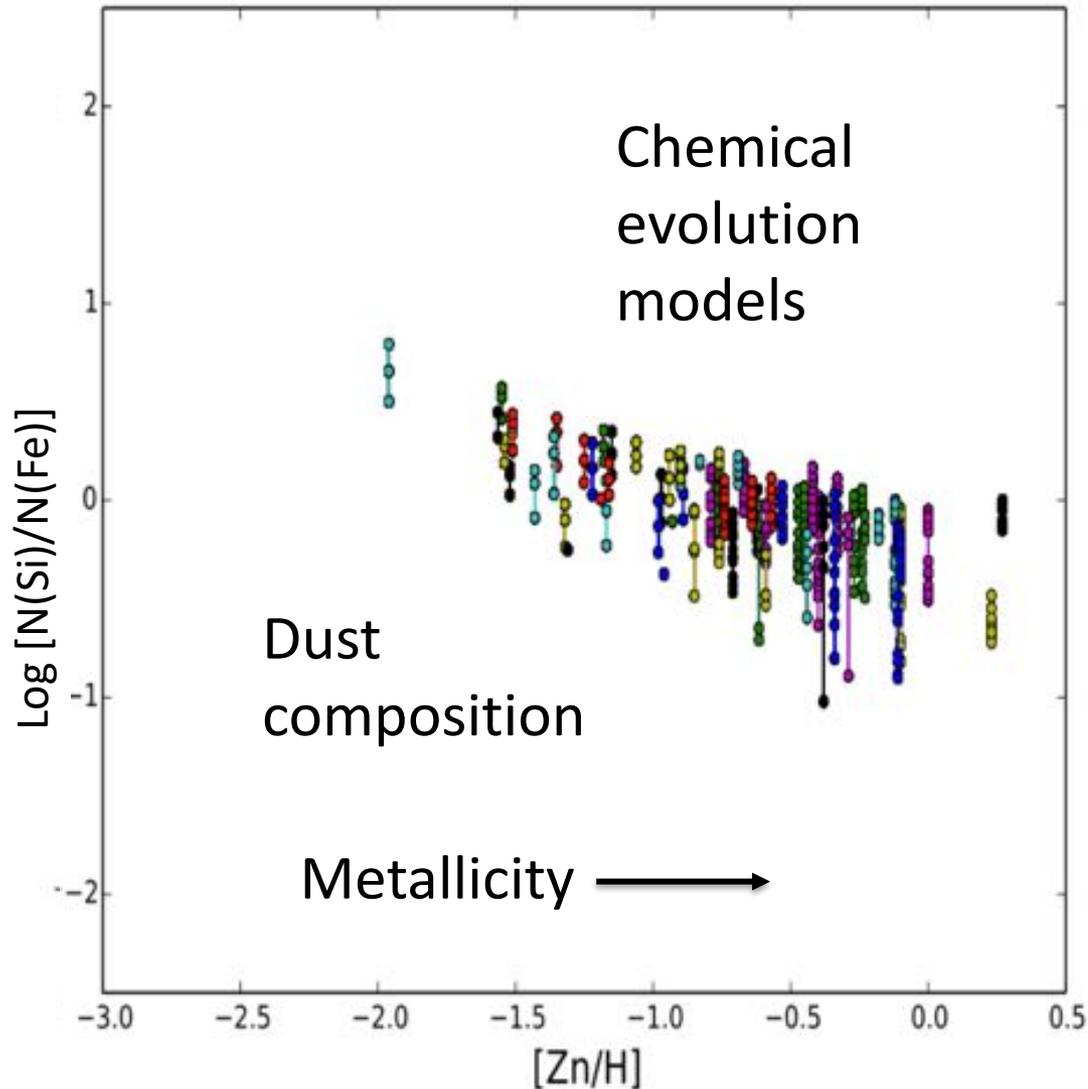
1. For each absorption system, what is the overall metallicity of the gas $[M/H]$ compared to solar abundances?
2. What proportion of the matter in the gas has condensed onto dust grains?
3. What is the overall behavior of the above two properties in various systems as a function of $z(\text{abs})$?

How this can be done

- Basic strategy: use differences in the rates of element depletions to differentiate between the effects of dust formation and low overall metallicities.
- A complication from chemical evolution: One must be aware of abundance differences between α -process and Fe-peak elements.

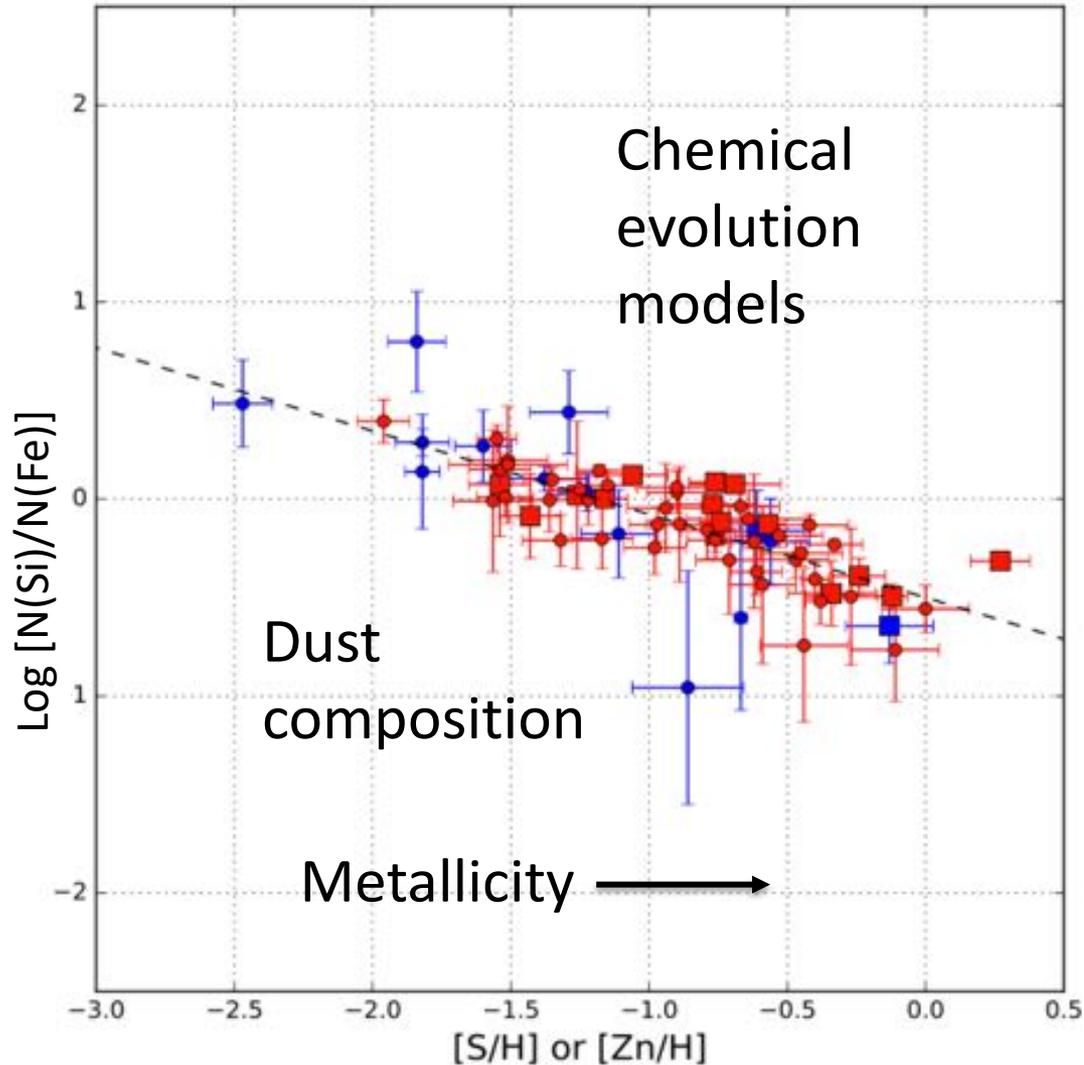


Behavior of $\log(\text{Si}/\text{Fe})_{\text{dust}}$ vs metallicity



Vladilo et al.
2018, ApJ,
868, 127

Behavior of $\log(\text{Si}/\text{Fe})_{\text{dust}}$ vs metallicity



Vladilo et al.
2018, ApJ,
868, 127

Recipe: Start with Depletion Coefficients

The basic equation:

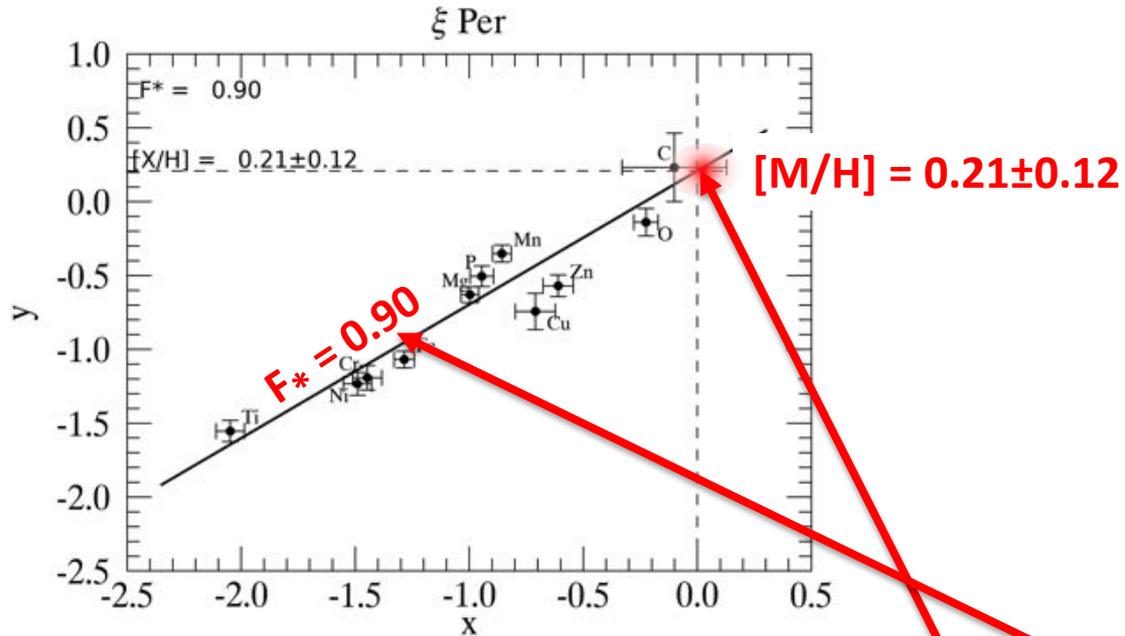
$$[X_{gas} / H] = B_X + A_X (F_* - z_X)$$

Elem. X	Log (X/H) _⊙ +12	A _X	B _X	z _X					
Elem. X (1)	Adopted (X/H) _⊙ ^b (2)	A _X (3)	B _X ^a (4)	z _X (5)	[X _{gas} /H] _⊙ ^a (6)	[X _{gas} /H] ₁ ^a (7)	χ ² (8)	r (9)	Prob. worse fit (10)
C	8.46 ± 0.04	-0.101 ± 0.229	-0.193 ± 0.060	0.803	-0.112 ± 0.194	-0.213 ± 0.075	3.7	8	0.881
N	7.90 ± 0.11	-0.000 ± 0.079	-0.109 ± 0.111	0.550	-0.109 ± 0.119	-0.109 ± 0.117	28.8	32	0.628
O	8.76 ± 0.05	-0.225 ± 0.053	-0.145 ± 0.051	0.598	-0.010 ± 0.060	-0.236 ± 0.055	75.0	64	0.164
Mg	7.62 ± 0.02	-0.997 ± 0.039	-0.800 ± 0.022	0.531	-0.270 ± 0.030	-1.267 ± 0.029	79.0	103	0.962
Si	7.61 ± 0.02	-1.136 ± 0.062	-0.570 ± 0.029	0.305	-0.223 ± 0.035	-1.359 ± 0.052	19.4	16	0.247
P	5.54 ± 0.04	-0.945 ± 0.051	-0.166 ± 0.042	0.488	0.296 ± 0.049	-0.649 ± 0.050	69.5	65	0.330
Cl	5.33 ± 0.06	-1.242 ± 0.129	-0.314 ± 0.065	0.609	0.442 ± 0.102	-0.800 ± 0.082	38.9	44	0.688
Ti	5.09 ± 0.03	-2.048 ± 0.062	-1.957 ± 0.033	0.430	-1.077 ± 0.043	-3.125 ± 0.049	50.7	43	0.195
Cr	5.72 ± 0.05	-1.447 ± 0.064	-1.508 ± 0.055	0.470	-0.827 ± 0.062	-2.274 ± 0.064	24.1	29	0.239
Mn	5.58 ± 0.03	-0.857 ± 0.041	-1.354 ± 0.032	0.520	-0.969 ± 0.038	-1.765 ± 0.038	106.3	83	0.043
Fe	7.54 ± 0.03	-1.285 ± 0.044	-1.513 ± 0.033	0.437	-0.951 ± 0.038	-2.236 ± 0.041	48.5	66	0.948
Ni	6.29 ± 0.03	-1.490 ± 0.062	-1.829 ± 0.035	0.599	-0.937 ± 0.051	-2.427 ± 0.043	30.7	34	0.630
Cu	4.34 ± 0.06	-0.710 ± 0.088	-1.102 ± 0.063	0.711	-0.597 ± 0.089	-1.307 ± 0.068	15.3	32	0.995
Zn	4.70 ± 0.04	-0.610 ± 0.066	-0.279 ± 0.045	0.555	0.059 ± 0.058	-0.551 ± 0.054	25.6	19	0.142
Ge	3.70 ± 0.05	-0.615 ± 0.083	-0.725 ± 0.054	0.690	-0.301 ± 0.078	-0.916 ± 0.059	12.4	24	0.975
Kr	3.36 ± 0.08	-0.166 ± 0.103	-0.332 ± 0.083	0.684	-0.218 ± 0.109	-0.584 ± 0.089	18.9	26	0.839

Recall that for any element
X in the ISM of our Galaxy,
its depletion is given by
But if the metallicity [M/H] of some
other system differs from that of our
Galaxy, we must add a new term

$$[X_{\text{gas}}/H] = \text{Log } N(X) - \text{Log } N(H) - \text{Log } (X/H)_{\odot} - [M/H] = B_X + A_X(F_* - z_X)$$

**Rearrange Terms in
this Formula**



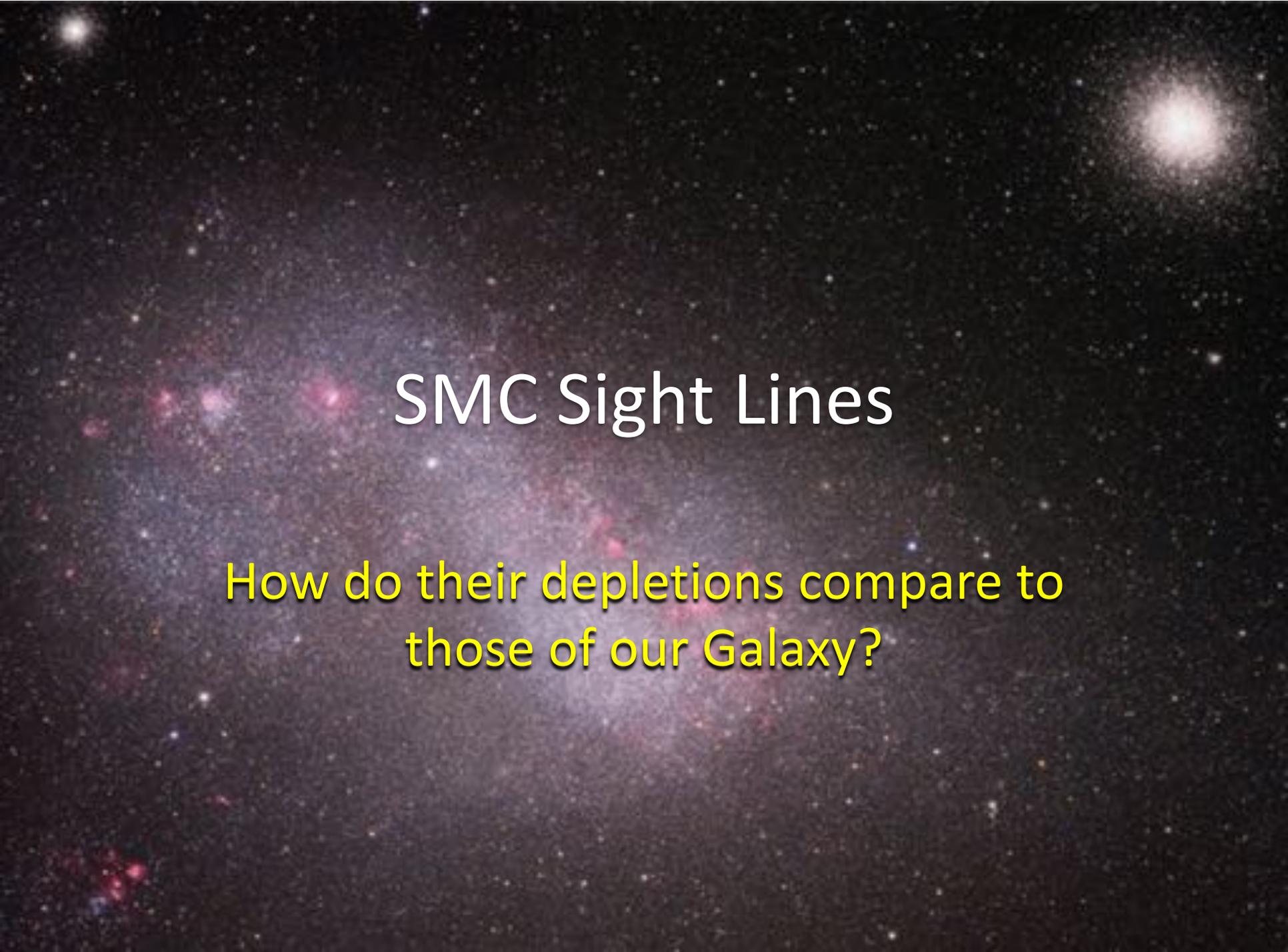
$$\underbrace{\left[\text{Log } N(X) - \text{Log } N(H) - \text{Log } (X/H)_{\odot} - B_X + A_X Z_X \right]}_y = \underbrace{[M/H]}_a + \underbrace{F^*}_b \underbrace{A_X}_x$$

These coefficients arise from a least squares best-fit equation for all X elements

SMC Sight Lines

Proof of concept:

Can we use interstellar absorption features to determine $[M/H]$ for the SMC, and if so, how does it compare with abundances in SMC stars?

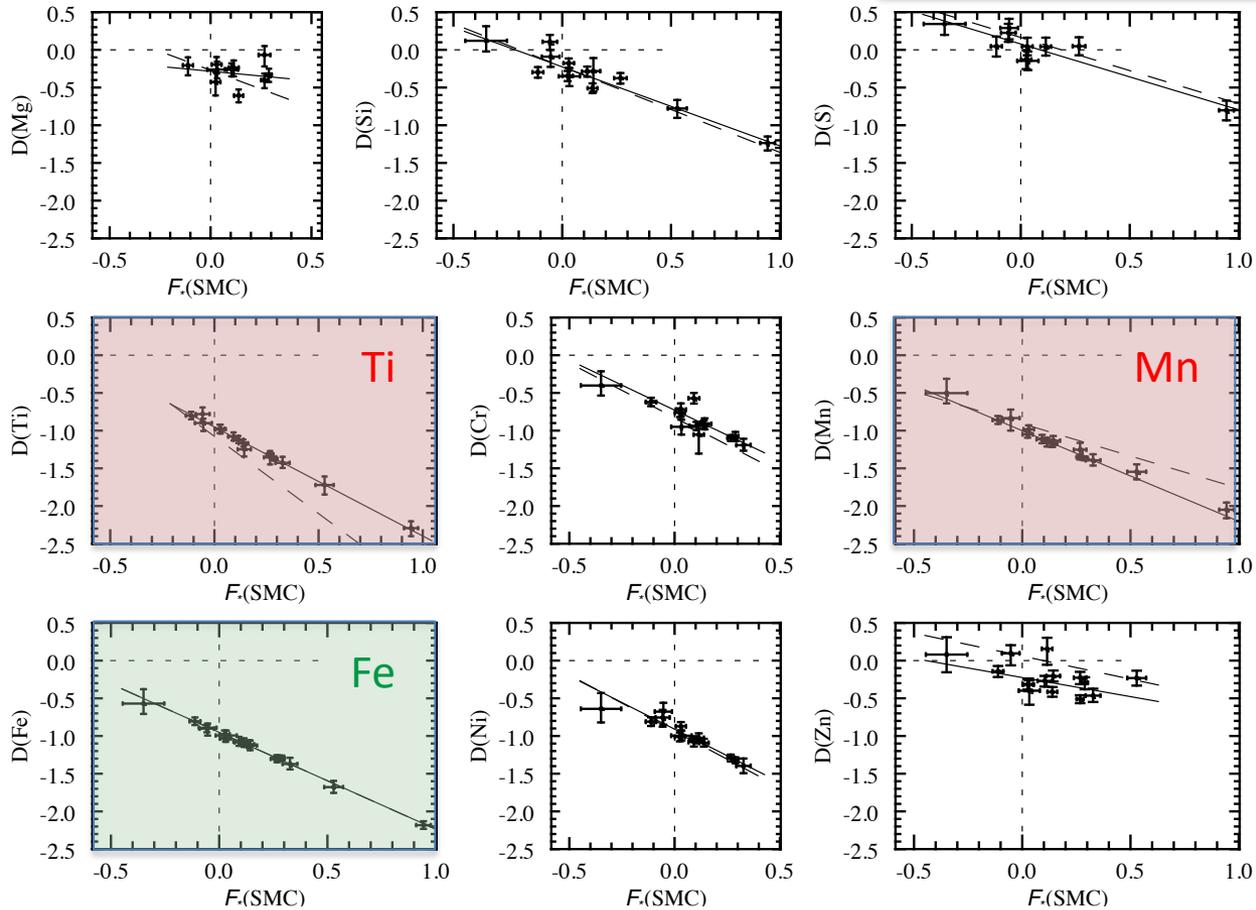


SMC Sight Lines

How do their depletions compare to those of our Galaxy?

Depletion trends with F_*

--- Milky Way trend
— SMC trend

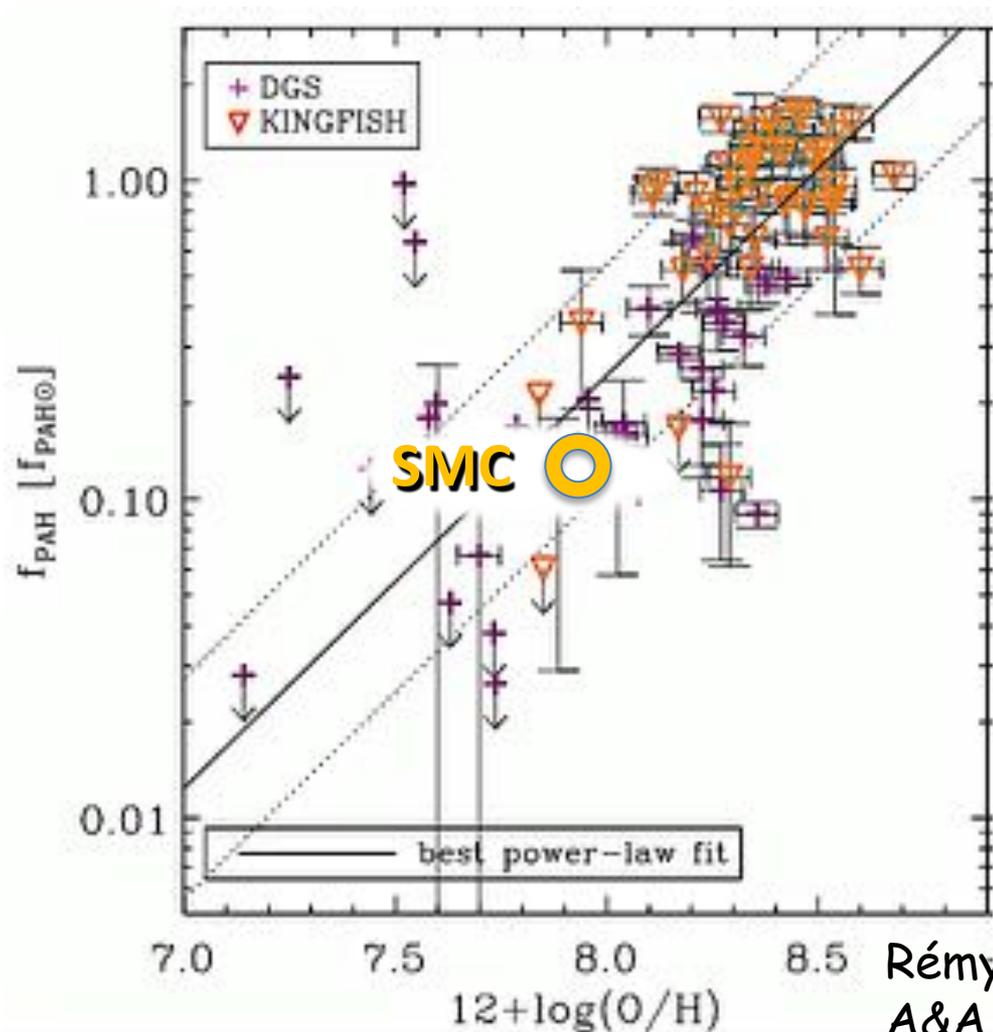


Jenkins & Wallerstein (2017, ApJ 838, 85)

Why do some of the SMC Depletions Differ from those of the Milky Way?

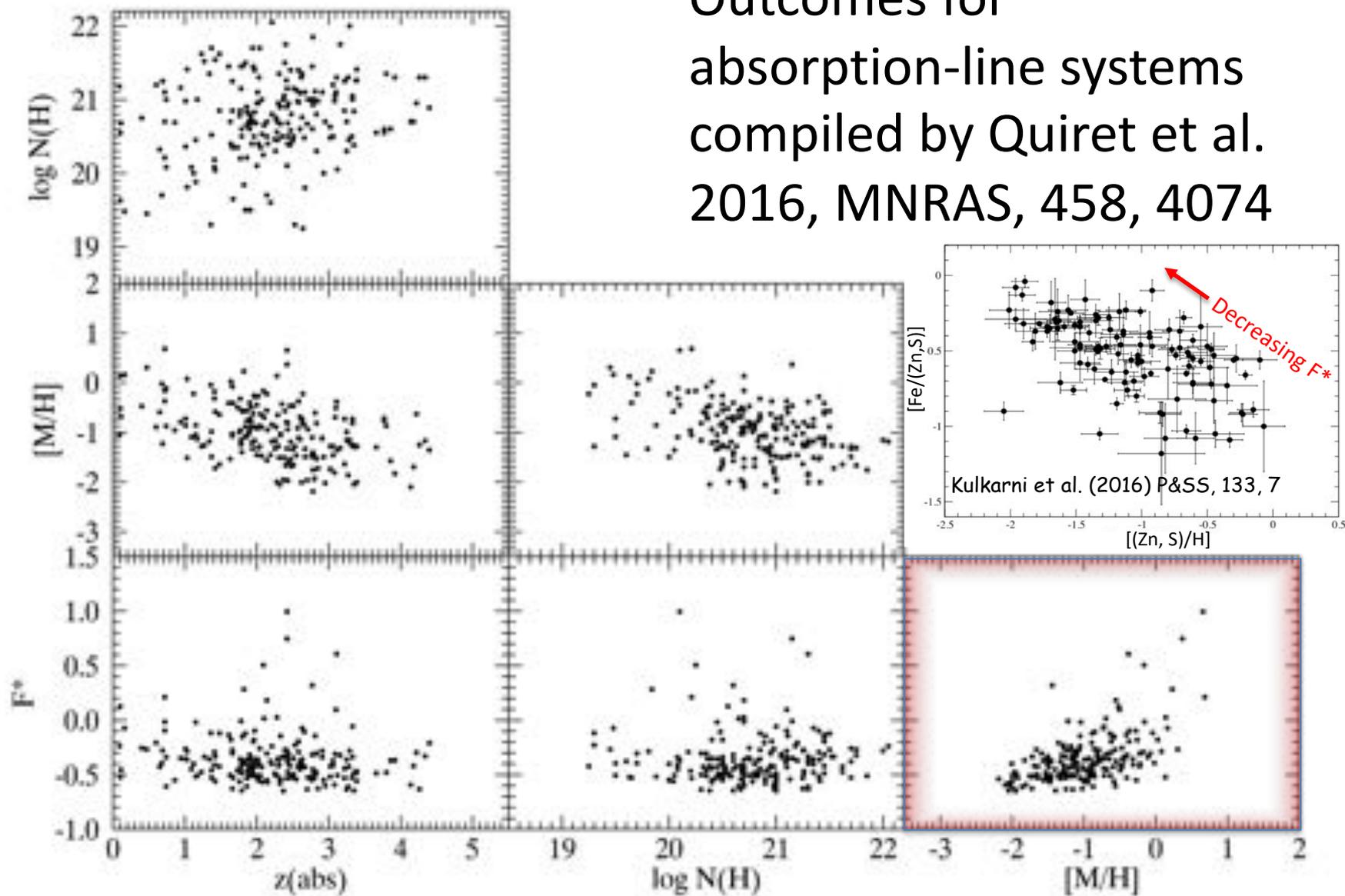
1. The stellar reference abundances of both α - and Fe-peak elements in the SMC are uniformly lower than those of the Milky Way by -0.65 dex.
2. So why does a gas with a dilute mixture of heavy elements exhibit a slightly different depletion behavior for Ti and Mn compared to that of Fe?
3. A possible answer: an exception to point 1 is the abundance of C in SMC stars is even lower by an additional -0.36 dex. This anomalously low C abundance is supported by a deficiency in PAHs, compared to the Milky Way PAH abundance.

The Relative Lack of Carbon in low metallicity systems (distant DLAs)

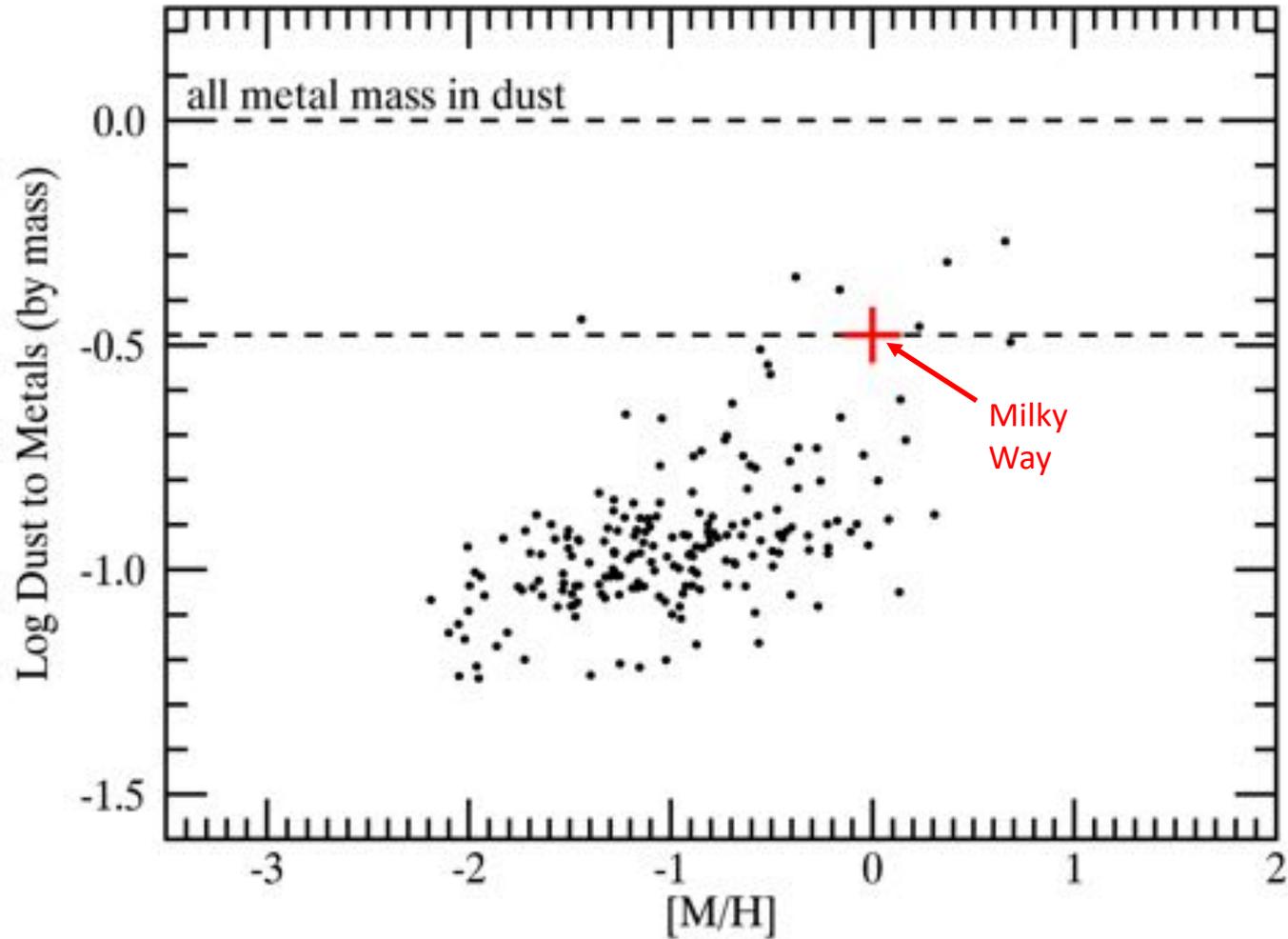


Rémy-Ruyer et al 2015,
A&A, 582, A121

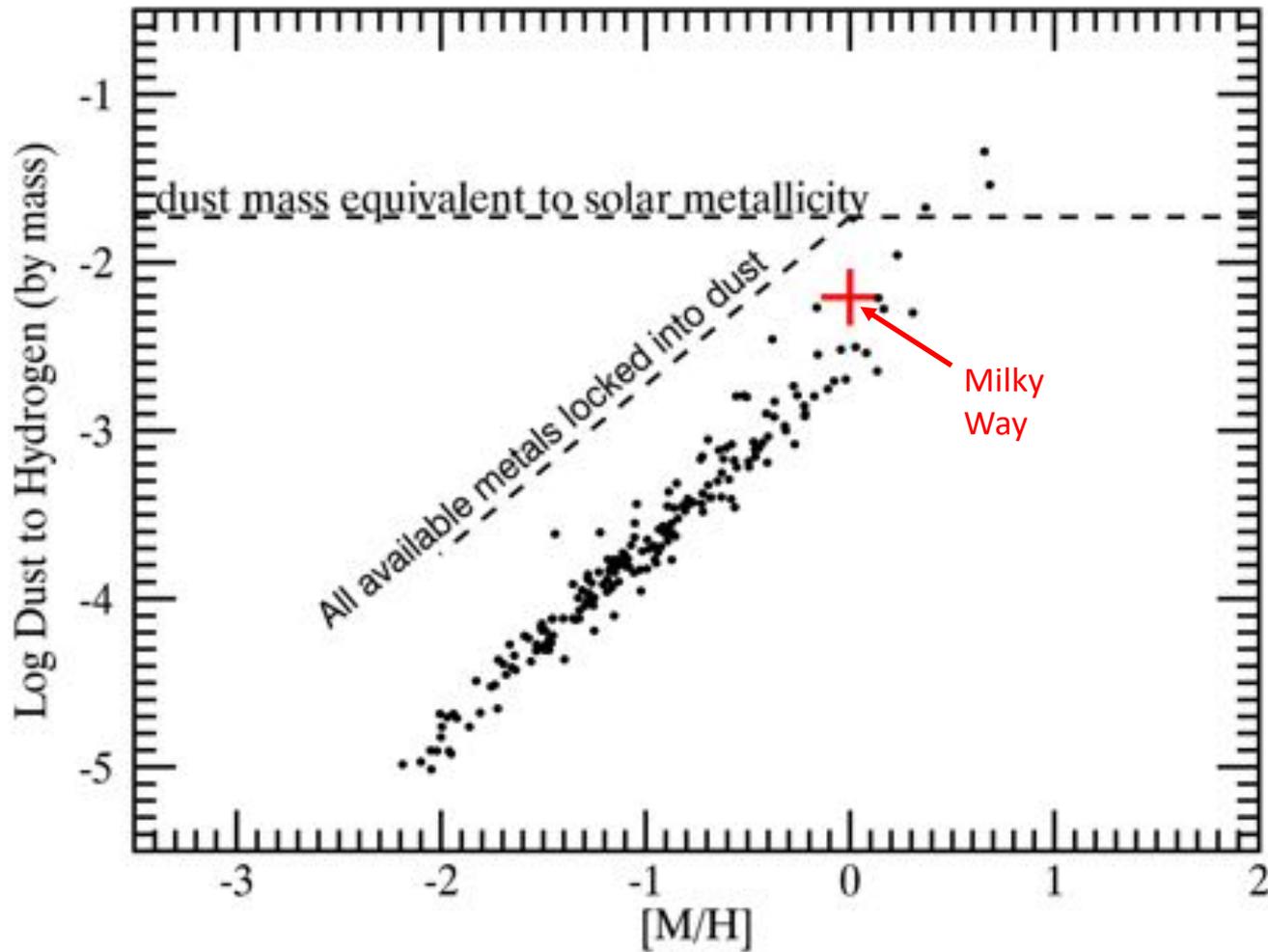
Outcomes for
absorption-line systems
compiled by Quiret et al.
2016, MNRAS, 458, 4074



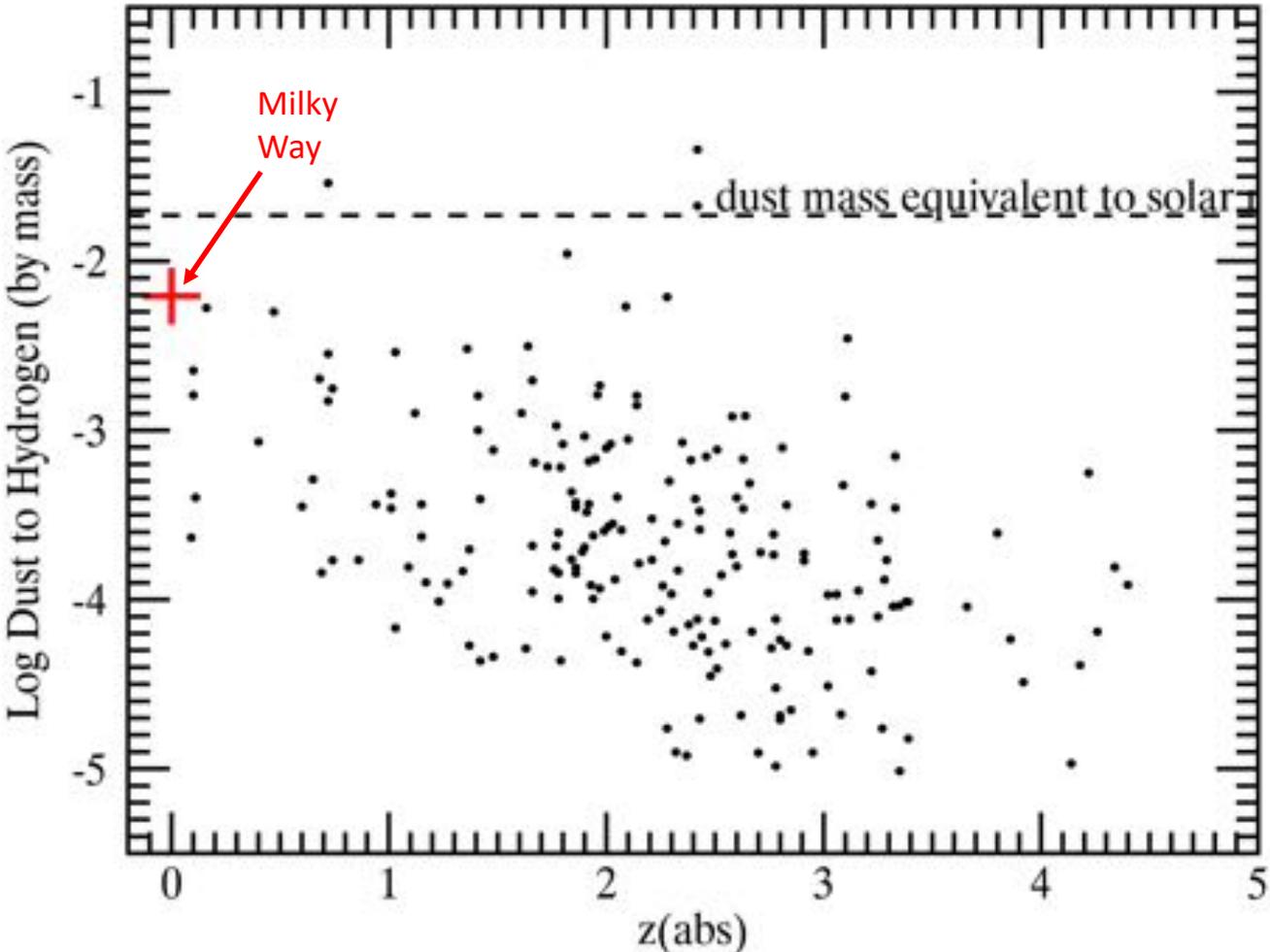
Mass Fractions of Heavy Elements in Dust



The Mass of Dust Relative to that of Hydrogen

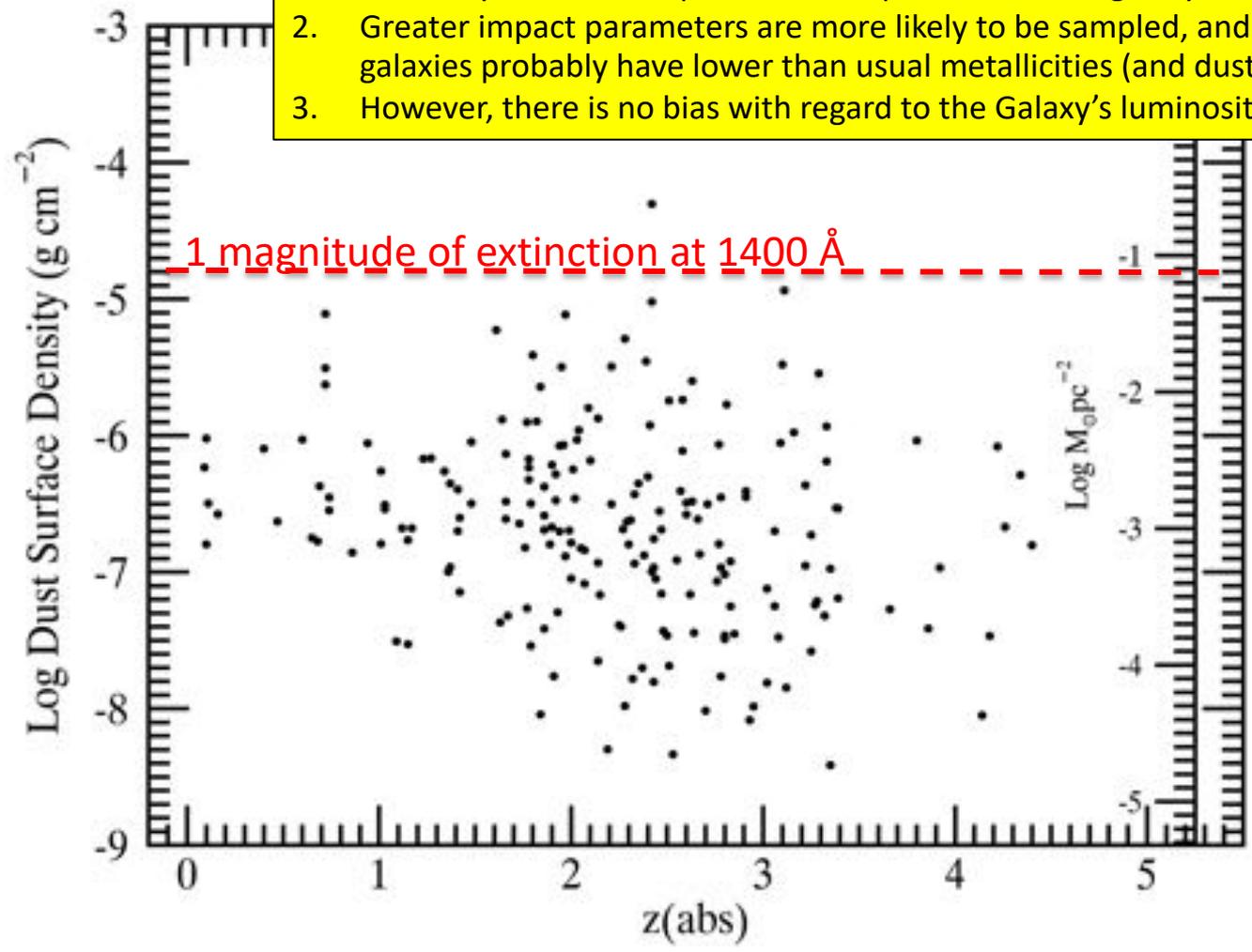


The Mass of Dust Relative to that of Hydrogen



Dust Surface Density and UV Opacity

- Selection biases:
1. Not likely to record a spectrum of a quasar behind a galaxy with a large extinction.
 2. Greater impact parameters are more likely to be sampled, and such locations in galaxies probably have lower than usual metallicities (and dust fractions).
 3. However, there is no bias with regard to the Galaxy's luminosity.



Summary

- UV Spectroscopy offers insights on the systematics of interstellar gas-phase abundances, which in turn informs us about the element constituents in solids
- There is a challenge in understanding the behaviors of oxygen and krypton
- From an almost universal pattern of depletions, we can use measurements of two or more elements to make corrections for depletions that are needed to derive element abundances in distant galaxies
- Depletion strengths and element abundances together reveal the absolute abundances of dust